

Esercizi su: Fattorizzazione di polinomi

1. Scomponi le seguenti differenze di quadrati.

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|---------------------|------------------------|
| (a) $x^2 - 9 =$ | $[(x - 3)(x + 3)]$ |
| (b) $x^2 - 9 =$ | $[(x - 3)(x + 3)]$ |
| (c) $x^2 - 1 =$ | $[(x - 1)(x + 1)]$ |
| (d) $x^2 - 81 =$ | $[(x - 9)(x + 9)]$ |
| (e) $x^2 - 49 =$ | $[(x - 7)(x + 7)]$ |
| (f) $x^2 - 144 =$ | $[(x - 12)(x + 12)]$ |
| (g) $4x^2 - 100 =$ | $[4(x - 5)(x + 5)]$ |
| (h) $4x^2 - 81 =$ | $[(2x - 9)(2x + 9)]$ |
| (i) $25x^2 - 25 =$ | $[25(x - 1)(x + 1)]$ |
| (j) $64x^2 - 64 =$ | $[64(x - 1)(x + 1)]$ |
| (k) $49x^2 - 49 =$ | $[49(x - 1)(x + 1)]$ |
| (l) $49x^2 - 49 =$ | $[49(x - 1)(x + 1)]$ |
| (m) $9x^2 - 64 =$ | $[(3x - 8)(3x + 8)]$ |
| (n) $64x^2 - 25 =$ | $[(8x - 5)(8x + 5)]$ |
| (o) $49x^2 - 36 =$ | $[(7x - 6)(7x + 6)]$ |
| (p) $49x^2 - 81 =$ | $[(7x - 9)(7x + 9)]$ |
| (q) $16x^2 - 4 =$ | $[4(2x - 1)(2x + 1)]$ |
| (r) $144x^2 - 9 =$ | $[9(4x - 1)(4x + 1)]$ |
| (s) $100x^2 - 9 =$ | $[(10x - 3)(10x + 3)]$ |
| (t) $64x^2 - 121 =$ | $[(8x - 11)(8x + 11)]$ |
| (u) $25x^2 - 144 =$ | $[(5x - 12)(5x + 12)]$ |
| (v) $64x^2 - 121 =$ | $[(8x - 11)(8x + 11)]$ |
| (w) $64x^2 - 144 =$ | $[16(2x - 3)(2x + 3)]$ |
| (x) $144x^2 - 16 =$ | $[16(3x - 1)(3x + 1)]$ |
| (y) $144x^2 - 64 =$ | $[16(3x - 2)(3x + 2)]$ |
| (z) $144x^2 - 64 =$ | $[16(3x - 2)(3x + 2)]$ |

2. Scomponi le seguenti differenze di quadrati.

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|-----------------------------|-----------------------------|
| (a) $x^2 - 81 =$ | $[(x - 9)(x + 9)]$ |
| (b) $16x^2 - 64 =$ | $[16(x - 2)(x + 2)]$ |
| (c) $\frac{x^2}{4} - 1 =$ | $[\frac{(x-2)(x+2)}{4}]$ |
| (d) $\frac{x^2}{4} - 1 =$ | $[\frac{(x-2)(x+2)}{4}]$ |
| (e) $\frac{x^2}{4} - 4 =$ | $[\frac{(x-4)(x+4)}{4}]$ |
| (f) $4x^2 - \frac{1}{9} =$ | $[\frac{(6x-1)(6x+1)}{9}]$ |
| (g) $x^2 - \frac{81}{16} =$ | $[\frac{(4x-9)(4x+9)}{16}]$ |
| (h) $9x^2 - \frac{16}{9} =$ | $[\frac{(9x-4)(9x+4)}{9}]$ |
| (i) $\frac{9x^2}{49} - 1 =$ | $[\frac{(3x-7)(3x+7)}{49}]$ |

- (j) $\frac{49x^2}{64} - 1 =$ $[\frac{(7x-8)(7x+8)}{64}]$
 (k) $\frac{49x^2}{4} - 36 =$ $[\frac{(7x-12)(7x+12)}{4}]$
 (l) $x^2 - \frac{144}{49} =$ $[\frac{(7x-12)(7x+12)}{49}]$
 (m) $16x^2 - \frac{1}{49} =$ $[\frac{(28x-1)(28x+1)}{49}]$
 (n) $\frac{25x^2}{49} - 4 =$ $[\frac{(5x-14)(5x+14)}{49}]$
 (o) $81x^2 - \frac{25}{16} =$ $[\frac{(36x-5)(36x+5)}{16}]$
 (p) $\frac{81x^2}{64} - 121 =$ $[\frac{(9x-88)(9x+88)}{64}]$
 (q) $36x^2 - \frac{9}{100} =$ $[\frac{9(20x-1)(20x+1)}{100}]$
 (r) $\frac{9x^2}{4} - \frac{81}{4} =$ $[\frac{9(x-3)(x+3)}{4}]$
 (s) $\frac{x^2}{4} - \frac{4}{49} =$ $[\frac{(7x-4)(7x+4)}{196}]$
 (t) $\frac{4x^2}{25} - \frac{1}{4} =$ $[\frac{(4x-5)(4x+5)}{100}]$
 (u) $\frac{25x^2}{64} - \frac{9}{4} =$ $[\frac{(5x-12)(5x+12)}{64}]$
 (v) $\frac{4x^2}{9} - \frac{36}{25} =$ $[\frac{4(5x-9)(5x+9)}{225}]$
 (w) $\frac{9x^2}{100} - \frac{4}{9} =$ $[\frac{(9x-20)(9x+20)}{900}]$
 (x) $\frac{9x^2}{16} - \frac{16}{25} =$ $[\frac{(15x-16)(15x+16)}{400}]$
 (y) $\frac{144x^2}{121} - \frac{36}{121} =$ $[\frac{36(2x-1)(2x+1)}{121}]$
 (z) $\frac{64x^2}{121} - \frac{144}{25} =$ $[\frac{16(10x-33)(10x+33)}{3025}]$

3. Trasforma i seguenti trinomi in quadrati di binomi.

- (a) $x^2 - 14x + 49 =$ $[(x-7)^2]$
 (b) $4x^2 - 36x + 81 =$ $[(2x-9)^2]$
 (c) $4x^2 - 16x + 16 =$ $[4(x-2)^2]$
 (d) $49x^2 - 42x + 9 =$ $[(7x-3)^2]$
 (e) $49x^2 - 42x + 9 =$ $[(7x-3)^2]$
 (f) $4x^2 + 36x + 81 =$ $[(2x+9)^2]$
 (g) $49x^2 + 14x + 1 =$ $[(7x+1)^2]$
 (h) $25x^2 - 80x + 64 =$ $[(5x-8)^2]$
 (i) $9x^2 - 72x + 144 =$ $[9(x-4)^2]$
 (j) $81x^2 - 90x + 25 =$ $[(9x-5)^2]$
 (k) $25x^2 - 40x + 16 =$ $[(5x-4)^2]$
 (l) $36x^2 + 72x + 36 =$ $[36(x+1)^2]$
 (m) $16x^2 - 64x + 64 =$ $[16(x-2)^2]$
 (n) $16x^2 - 48x + 36 =$ $[4(2x-3)^2]$
 (o) $36x^2 + 48x + 16 =$ $[4(3x+2)^2]$
 (p) $16x^2 - 88x + 121 =$ $[(4x-11)^2]$
 (q) $81x^2 + 162x + 81 =$ $[81(x+1)^2]$
 (r) $16x^2 - 88x + 121 =$ $[(4x-11)^2]$
 (s) $100x^2 + 180x + 81 =$ $[(10x+9)^2]$

- (t) $121x^2 - 132x + 36 =$ $[(11x - 6)^2]$
 (u) $64x^2 + 176x + 121 =$ $[(8x + 11)^2]$
 (v) $100x^2 + 180x + 81 =$ $[(10x + 9)^2]$
 (w) $81x^2 + 216x + 144 =$ $[9(3x + 4)^2]$
 (x) $64x^2 - 192x + 144 =$ $[16(2x - 3)^2]$
 (y) $144x^2 + 144x + 36 =$ $[36(2x + 1)^2]$
 (z) $144x^2 - 144x + 36 =$ $[36(2x - 1)^2]$

4. Trasforma i seguenti trinomi in quadrati di binomi.

- (a) $x^2 + 18x + 81 =$ $[(x + 9)^2]$
 (b) $9x^2 - 9x + \frac{9}{4} =$ $[\frac{9(2x-1)^2}{4}]$
 (c) $36x^2 - 8x + \frac{4}{9} =$ $[\frac{4(9x-1)^2}{9}]$
 (d) $100x^2 - 12x + \frac{9}{25} =$ $[\frac{(50x-3)^2}{25}]$
 (e) $\frac{x^2}{9} - \frac{2x}{3} + 1 =$ $[\frac{(x-3)^2}{9}]$
 (f) $144x^2 - 32x + \frac{16}{9} =$ $[\frac{16(9x-1)^2}{9}]$
 (g) $x^2 + \frac{2x}{3} + \frac{1}{9} =$ $[\frac{(3x+1)^2}{9}]$
 (h) $\frac{4x^2}{9} - \frac{4x}{3} + 1 =$ $[\frac{(2x-3)^2}{9}]$
 (i) $\frac{81x^2}{100} + 18x + 100 =$ $[\frac{(9x+100)^2}{100}]$
 (j) $\frac{25x^2}{9} - \frac{50x}{3} + 25 =$ $[\frac{25(x-3)^2}{9}]$
 (k) $\frac{49x^2}{81} - \frac{28x}{9} + 4 =$ $[\frac{(7x-18)^2}{81}]$
 (l) $16x^2 + \frac{72x}{5} + \frac{81}{25} =$ $[\frac{(20x+9)^2}{25}]$
 (m) $64x^2 - \frac{40x}{3} + \frac{25}{36} =$ $[\frac{(48x-5)^2}{36}]$
 (n) $\frac{x^2}{4} - \frac{x}{5} + \frac{1}{25} =$ $[\frac{(5x-2)^2}{100}]$
 (o) $\frac{4x^2}{9} - \frac{2x}{3} + \frac{1}{4} =$ $[\frac{(4x-3)^2}{36}]$
 (p) $\frac{x^2}{16} + \frac{11x}{8} + \frac{121}{16} =$ $[\frac{(x+11)^2}{16}]$
 (q) $\frac{9x^2}{16} - \frac{9x}{8} + \frac{9}{16} =$ $[\frac{9(x-1)^2}{16}]$
 (r) $\frac{16x^2}{81} + \frac{8x}{27} + \frac{1}{9} =$ $[\frac{(4x+3)^2}{81}]$
 (s) $\frac{81x^2}{4} - \frac{9x}{8} + \frac{1}{64} =$ $[\frac{(36x-1)^2}{64}]$
 (t) $\frac{9x^2}{4} + \frac{8x}{3} + \frac{64}{81} =$ $[\frac{(27x+16)^2}{324}]$
 (u) $\frac{9x^2}{4} + \frac{7x}{3} + \frac{49}{81} =$ $[\frac{(27x+14)^2}{324}]$
 (v) $\frac{9x^2}{25} - \frac{3x}{25} + \frac{1}{100} =$ $[\frac{(6x-1)^2}{100}]$
 (w) $\frac{9x^2}{49} - \frac{9x}{14} + \frac{9}{16} =$ $[\frac{9(4x-7)^2}{784}]$
 (x) $\frac{9x^2}{100} - \frac{x}{20} + \frac{1}{144} =$ $[\frac{(18x-5)^2}{3600}]$
 (y) $\frac{121x^2}{16} + \frac{33x}{10} + \frac{9}{25} =$ $[\frac{(55x+12)^2}{400}]$
 (z) $\frac{121x^2}{144} + \frac{121x}{18} + \frac{121}{9} =$ $[\frac{121(x+4)^2}{144}]$

5. Scomponi i seguenti quadrati di trinomi.

- (a) $x^4 + 8x^3 + 24x^2 + 32x + 16 =$ $[(x+2)^4]$
 (b) $9x^4 - 36x^3 + 54x^2 - 36x + 9 =$ $[9(x-1)^4]$
 (c) $x^4 + 2x^3 + 9x^2 + 8x + 16 =$ $[(x^2 + x + 4)^2]$
 (d) $x^4 + 2x^3 + 11x^2 + 10x + 25 =$ $[(x^2 + x + 5)^2]$
 (e) $4x^4 + 4x^3 + 25x^2 + 12x + 36 =$ $[(2x^2 + x + 6)^2]$
 (f) $36x^4 + 12x^3 + 37x^2 + 6x + 9 =$ $[(6x^2 + x + 3)^2]$
 (g) $9x^4 - 18x^3 + 27x^2 - 18x + 9 =$ $[9(x^2 - x + 1)^2]$
 (h) $16x^4 + 8x^3 + 41x^2 + 10x + 25 =$ $[(4x^2 + x + 5)^2]$
 (i) $4x^4 - 20x^3 + 9x^2 + 40x + 16 =$ $[(2x^2 - 5x - 4)^2]$
 (j) $16x^4 - 16x^3 + 20x^2 - 8x + 4 =$ $[4(2x^2 - x + 1)^2]$
 (k) $4x^4 + 16x^3 - 4x^2 - 40x + 25 =$ $[(2x^2 + 4x - 5)^2]$
 (l) $36x^4 - 12x^3 + 61x^2 - 10x + 25 =$ $[(6x^2 - x + 5)^2]$
 (m) $4x^4 + 24x^3 + 32x^2 - 12x + 1 =$ $[(2x^2 + 6x - 1)^2]$
 (n) $9x^4 - 18x^3 + 33x^2 - 24x + 16 =$ $[(3x^2 - 3x + 4)^2]$
 (o) $25x^4 - 40x^3 + 46x^2 - 24x + 9 =$ $[(5x^2 - 4x + 3)^2]$
 (p) $9x^4 + 12x^3 - 32x^2 - 24x + 36 =$ $[(3x^2 + 2x - 6)^2]$
 (q) $36x^4 + 36x^3 - 15x^2 - 12x + 4 =$ $[(6x^2 + 3x - 2)^2]$
 (r) $25x^4 + 40x^3 - 24x^2 - 32x + 16 =$ $[(5x^2 + 4x - 4)^2]$
 (s) $36x^4 - 24x^3 - 68x^2 + 24x + 36 =$ $[4(3x^2 - x - 3)^2]$
 (t) $25x^4 + 40x^3 - 34x^2 - 40x + 25 =$ $[(5x^2 + 4x - 5)^2]$
 (u) $4x^4 - 4x^3 - 3x^2 + 2x + 1 =$ $[(x-1)^2(2x+1)^2]$
 (v) $4x^4 - 12x^3 + x^2 + 12x + 4 =$ $[(x-2)^2(2x+1)^2]$
 (w) $4x^4 - 4x^3 - 11x^2 + 6x + 9 =$ $[(x+1)^2(2x-3)^2]$
 (x) $4x^4 + 12x^3 + 13x^2 + 6x + 1 =$ $[(x+1)^2(2x+1)^2]$
 (y) $9x^4 - 24x^3 - 8x^2 + 32x + 16 =$ $[(x-2)^2(3x+2)^2]$
 (z) $16x^4 + 16x^3 - 44x^2 - 24x + 36 =$ $[4(x-1)^2(2x+3)^2]$

6. Scomponi i seguenti quadrati di trinomi.

- (a) $x^4 - 6x^3 + 7x^2 + 6x + 1 =$ $[(x^2 - 3x - 1)^2]$
 (b) $x^4 - x^3 + \frac{49x^2}{4} - 6x + 36 =$ $[\frac{(2x^2 - x + 12)^2}{4}]$
 (c) $\frac{x^4}{4} - 2x^3 + 7x^2 - 12x + 9 =$ $[\frac{(x^2 - 4x + 6)^2}{4}]$
 (d) $16x^4 + 2x^3 - \frac{255x^2}{16} - x + 4 =$ $[\frac{(16x^2 + x - 8)^2}{16}]$
 (e) $36x^4 - 30x^3 - \frac{71x^2}{4} + 10x + 4 =$ $[\frac{(12x^2 - 5x - 4)^2}{4}]$
 (f) $\frac{4x^4}{25} + 4x^3 + \frac{149x^2}{5} + 60x + 36 =$ $[\frac{(2x^2 + 25x + 30)^2}{25}]$
 (g) $4x^4 - \frac{4x^3}{3} - \frac{71x^2}{9} + \frac{4x}{3} + 4 =$ $[\frac{(6x^2 - x - 6)^2}{9}]$
 (h) $x^4 + \frac{4x^3}{5} + \frac{54x^2}{25} + \frac{4x}{5} + 1 =$ $[\frac{(5x^2 + 2x + 5)^2}{25}]$

- (i) $x^4 - 3x^3 + \frac{19x^2}{4} - \frac{15x}{4} + \frac{25}{16} =$ $[\frac{(4x^2-6x+5)^2}{16}]$
- (j) $25x^4 - 20x^3 + \frac{2x^2}{3} + \frac{4x}{3} + \frac{1}{9} =$ $[\frac{(15x^2-6x-1)^2}{9}]$
- (k) $\frac{9x^4}{16} - x^3 - \frac{65x^2}{36} + 2x + \frac{9}{4} =$ $[\frac{(9x^2-8x-18)^2}{144}]$
- (l) $x^4 - 4x^3 + \frac{28x^2}{5} - \frac{16x}{5} + \frac{16}{25} =$ $[\frac{(5x^2-10x+4)^2}{25}]$
- (m) $\frac{x^4}{9} - 4x^3 + \frac{319x^2}{9} + 10x + \frac{25}{36} =$ $[\frac{(2x^2-36x-5)^2}{36}]$
- (n) $\frac{x^4}{36} + \frac{x^3}{4} + \frac{43x^2}{48} + \frac{3x}{2} + 1 =$ $[\frac{(2x^2+9x+12)^2}{144}]$
- (o) $\frac{4x^4}{9} + \frac{8x^3}{9} + \frac{13x^2}{9} + x + \frac{9}{16} =$ $[\frac{(8x^2+8x+9)^2}{144}]$
- (p) $\frac{x^4}{4} - \frac{3x^3}{2} + \frac{47x^2}{12} - 5x + \frac{25}{9} =$ $[\frac{(3x^2-9x+10)^2}{36}]$
- (q) $\frac{9x^4}{25} + \frac{2x^3}{5} - \frac{49x^2}{45} - \frac{2x}{3} + 1 =$ $[\frac{(9x^2+5x-15)^2}{225}]$
- (r) $16x^4 + \frac{8x^3}{3} + \frac{61x^2}{9} + \frac{5x}{9} + \frac{25}{36} =$ $[\frac{(24x^2+2x+5)^2}{36}]$
- (s) $\frac{4x^4}{9} + \frac{4x^3}{9} + \frac{5x^2}{9} + \frac{2x}{9} + \frac{1}{9} =$ $[\frac{(2x^2+x+1)^2}{9}]$
- (t) $36x^4 - 2x^3 - \frac{143x^2}{36} + \frac{x}{9} + \frac{1}{9} =$ $[\frac{(4x-1)^2(9x+2)^2}{36}]$
- (u) $\frac{4x^4}{9} - \frac{8x^3}{5} + \frac{308x^2}{75} - \frac{24x}{5} + 4 =$ $[\frac{4(5x^2-9x+15)^2}{225}]$
- (v) $\frac{25x^4}{4} + 4x^3 - \frac{202x^2}{75} - \frac{16x}{15} + \frac{4}{9} =$ $[\frac{(75x^2+24x-20)^2}{900}]$
- (w) $\frac{16x^4}{9} + \frac{4x^3}{3} + \frac{19x^2}{12} + \frac{x}{2} + \frac{1}{4} =$ $[\frac{(8x^2+3x+3)^2}{36}]$
- (x) $\frac{x^4}{4} + \frac{x^3}{4} - \frac{77x^2}{48} - \frac{5x}{6} + \frac{25}{9} =$ $[\frac{(6x^2+3x-20)^2}{144}]$
- (y) $\frac{9x^4}{25} + \frac{x^3}{5} + \frac{73x^2}{36} + \frac{5x}{9} + \frac{25}{9} =$ $[\frac{(18x^2+5x+50)^2}{900}]$
- (z) $\frac{4x^4}{25} - \frac{8x^3}{5} + \frac{96x^2}{25} + \frac{4x}{5} + \frac{1}{25} =$ $[\frac{(2x^2-10x-1)^2}{25}]$

7. Scomponi i seguenti trinomi notevoli.

- (a) $x^2 + 8x + 16 =$ $[(x + 4)^2]$
- (b) $x^2 + 12x + 36 =$ $[(x + 6)^2]$
- (c) $x^2 + 12x + 36 =$ $[(x + 6)^2]$
- (d) $x^2 + 14x + 49 =$ $[(x + 7)^2]$
- (e) $x^2 - 49 =$ $[(x - 7)(x + 7)]$
- (f) $x^2 - 5x + 4 =$ $[(x - 4)(x - 1)]$
- (g) $x^2 - 2x - 3 =$ $[(x - 3)(x + 1)]$
- (h) $x^2 + 2x - 24 =$ $[(x - 4)(x + 6)]$
- (i) $x^2 - 5x - 36 =$ $[(x - 9)(x + 4)]$
- (j) $x^2 - 6x - 27 =$ $[(x - 9)(x + 3)]$
- (k) $x^2 - 4x - 45 =$ $[(x - 9)(x + 5)]$
- (l) $x^2 - 10x + 9 =$ $[(x - 9)(x - 1)]$
- (m) $x^2 - 3x - 10 =$ $[(x - 5)(x + 2)]$
- (n) $x^2 - 2x - 24 =$ $[(x - 6)(x + 4)]$
- (o) $x^2 + 3x - 10 =$ $[(x - 2)(x + 5)]$

- (p) $x^2 - 7x - 44 =$ $[(x - 11)(x + 4)]$
 (q) $x^2 - 6x - 55 =$ $[(x - 11)(x + 5)]$
 (r) $x^2 - 8x - 33 =$ $[(x - 11)(x + 3)]$
 (s) $x^2 + 6x - 40 =$ $[(x - 4)(x + 10)]$
 (t) $x^2 + 14x + 45 =$ $[(x + 5)(x + 9)]$
 (u) $x^2 + 3x - 70 =$ $[(x - 7)(x + 10)]$
 (v) $x^2 + 7x - 44 =$ $[(x - 4)(x + 11)]$
 (w) $x^2 - 2x - 99 =$ $[(x - 11)(x + 9)]$
 (x) $x^2 - 20x + 99 =$ $[(x - 11)(x - 9)]$
 (y) $x^2 - 15x + 36 =$ $[(x - 12)(x - 3)]$
 (z) $x^2 + 13x + 22 =$ $[(x + 2)(x + 11)]$

8. Scomponi i seguenti trinomi notevoli.

- (a) $x^2 + 3x + 2 =$ $[(x + 1)(x + 2)]$
 (b) $x^2 - 2x + \frac{5}{9} =$ $[\frac{(3x-5)(3x-1)}{9}]$
 (c) $x^2 + 2x + \frac{3}{4} =$ $[\frac{(2x+1)(2x+3)}{4}]$
 (d) $x^2 - \frac{x}{4} - \frac{3}{4} =$ $[\frac{(x-1)(4x+3)}{4}]$
 (e) $x^2 - \frac{8x}{5} + \frac{3}{5} =$ $[\frac{(x-1)(5x-3)}{5}]$
 (f) $x^2 + \frac{7x}{6} + \frac{1}{6} =$ $[\frac{(x+1)(6x+1)}{6}]$
 (g) $x^2 + \frac{17x}{6} + \frac{5}{3} =$ $[\frac{(x+2)(6x+5)}{6}]$
 (h) $x^2 - \frac{13x}{6} + \frac{7}{6} =$ $[\frac{(x-1)(6x-7)}{6}]$
 (i) $x^2 - \frac{14x}{3} + \frac{8}{3} =$ $[\frac{(x-4)(3x-2)}{3}]$
 (j) $x^2 - \frac{45x}{7} + \frac{18}{7} =$ $[\frac{(x-6)(7x-3)}{7}]$
 (k) $x^2 - \frac{5x}{4} - \frac{3}{8} =$ $[\frac{(2x-3)(4x+1)}{8}]$
 (l) $x^2 + \frac{22x}{5} + \frac{21}{5} =$ $[\frac{(x+3)(5x+7)}{5}]$
 (m) $x^2 + \frac{11x}{9} - \frac{14}{9} =$ $[\frac{(x+2)(9x-7)}{9}]$
 (n) $x^2 - \frac{11x}{10} - \frac{9}{5} =$ $[\frac{(x-2)(10x+9)}{10}]$
 (o) $x^2 - \frac{3x}{8} - \frac{7}{16} =$ $[\frac{(2x+1)(8x-7)}{16}]$
 (p) $x^2 - \frac{49x}{10} + \frac{9}{5} =$ $[\frac{(2x-9)(5x-2)}{10}]$
 (q) $x^2 + \frac{41x}{15} + \frac{4}{5} =$ $[\frac{(3x+1)(5x+12)}{15}]$
 (r) $x^2 + \frac{17x}{12} + \frac{1}{9} =$ $[\frac{(3x+4)(12x+1)}{36}]$
 (s) $x^2 + \frac{23x}{45} + \frac{2}{45} =$ $[\frac{(5x+2)(9x+1)}{45}]$
 (t) $x^2 - \frac{17x}{21} - \frac{10}{7} =$ $[\frac{(3x-5)(7x+6)}{21}]$
 (u) $x^2 + \frac{13x}{18} + \frac{5}{54} =$ $[\frac{(6x+1)(9x+5)}{54}]$
 (v) $x^2 - \frac{5x}{3} + \frac{11}{16} =$ $[\frac{(4x-3)(12x-11)}{48}]$
 (w) $x^2 + \frac{13x}{5} + \frac{33}{20} =$ $[\frac{(2x+3)(10x+11)}{20}]$
 (x) $x^2 - \frac{x}{11} - \frac{56}{121} =$ $[\frac{(11x-8)(11x+7)}{121}]$
 (y) $x^2 - \frac{51x}{20} - \frac{11}{20} =$ $[\frac{(4x-11)(5x+1)}{20}]$

$$(z) \quad x^2 + \frac{75x}{28} + \frac{25}{14} = \boxed{\frac{(4x+5)(7x+10)}{28}}$$

9. Scomponi i seguenti cubi di binomi.

- | | |
|---------------------------------------|-----------------|
| (a) $x^3 + 15x^2 + 75x + 125 =$ | $[(x+5)^3]$ |
| (b) $x^3 - 18x^2 + 108x - 216 =$ | $[(x-6)^3]$ |
| (c) $8x^3 + 24x^2 + 24x + 8 =$ | $[8(x+1)^3]$ |
| (d) $64x^3 + 48x^2 + 12x + 1 =$ | $[(4x+1)^3]$ |
| (e) $27x^3 + 54x^2 + 36x + 8 =$ | $[(3x+2)^3]$ |
| (f) $27x^3 - 54x^2 + 36x - 8 =$ | $[(3x-2)^3]$ |
| (g) $-x^3 - 15x^2 - 75x - 125 =$ | $[-(x+5)^3]$ |
| (h) $64x^3 + 96x^2 + 48x + 8 =$ | $[8(2x+1)^3]$ |
| (i) $8x^3 - 60x^2 + 150x - 125 =$ | $[(2x-5)^3]$ |
| (j) $-8x^3 + 12x^2 - 6x + 1 =$ | $[-(2x-1)^3]$ |
| (k) $-27x^3 + 27x^2 - 9x + 1 =$ | $[-(3x-1)^3]$ |
| (l) $-27x^3 - 27x^2 - 9x - 1 =$ | $[-(3x+1)^3]$ |
| (m) $216x^3 - 216x^2 + 72x - 8 =$ | $[8(3x-1)^3]$ |
| (n) $-125x^3 + 75x^2 - 15x + 1 =$ | $[-(5x-1)^3]$ |
| (o) $-125x^3 + 75x^2 - 15x + 1 =$ | $[-(5x-1)^3]$ |
| (p) $216x^3 - 540x^2 + 450x - 125 =$ | $[(6x-5)^3]$ |
| (q) $-8x^3 + 72x^2 - 216x + 216 =$ | $[-8(x-3)^3]$ |
| (r) $-8x^3 + 60x^2 - 150x + 125 =$ | $[-(2x-5)^3]$ |
| (s) $-8x^3 - 72x^2 - 216x - 216 =$ | $[-8(x+3)^3]$ |
| (t) $216x^3 + 432x^2 + 288x + 64 =$ | $[8(3x+2)^3]$ |
| (u) $-125x^3 + 150x^2 - 60x + 8 =$ | $[-(5x-2)^3]$ |
| (v) $216x^3 - 324x^2 + 162x - 27 =$ | $[27(2x-1)^3]$ |
| (w) $-125x^3 + 225x^2 - 135x + 27 =$ | $[-(5x-3)^3]$ |
| (x) $-64x^3 + 192x^2 - 192x + 64 =$ | $[-64(x-1)^3]$ |
| (y) $-216x^3 + 432x^2 - 288x + 64 =$ | $[-8(3x-2)^3]$ |
| (z) $-216x^3 + 648x^2 - 648x + 216 =$ | $[-216(x-1)^3]$ |

10. Scomponi i seguenti cubi di binomi.

- | | |
|--|--------------------------|
| (a) $x^3 + 3x^2 + 3x + 1 =$ | $[(x+1)^3]$ |
| (b) $x^3 + 12x^2 + 48x + 64 =$ | $[(x+4)^3]$ |
| (c) $-x^3 - 3x^2 - 3x - 1 =$ | $[-(x+1)^3]$ |
| (d) $64x^3 - 48x^2 + 12x - 1 =$ | $[(4x-1)^3]$ |
| (e) $-8x^3 - 48x^2 - 96x - 64 =$ | $[-8(x+2)^3]$ |
| (f) $216x^3 + 540x^2 + 450x + 125 =$ | $[(6x+5)^3]$ |
| (g) $27x^3 + 45x^2 + 25x + \frac{125}{27} =$ | $[\frac{(9x+5)^3}{27}]$ |
| (h) $8x^3 - 8x^2 + \frac{8x}{3} - \frac{8}{27} =$ | $[\frac{8(3x-1)^3}{27}]$ |
| (i) $-\frac{27x^3}{8} - \frac{27x^2}{2} - 18x - 8 =$ | $[-\frac{(3x+4)^3}{8}]$ |

- (j) $-8x^3 + 9x^2 - \frac{27x}{8} + \frac{27}{64} =$ $[-\frac{(8x-3)^3}{64}]$
- (k) $\frac{x^3}{125} + \frac{3x^2}{25} + \frac{3x}{5} + 1 =$ $[\frac{(x+5)^3}{125}]$
- (l) $\frac{27x^3}{8} + \frac{27x^2}{4} + \frac{9x}{2} + 1 =$ $[\frac{(3x+2)^3}{8}]$
- (m) $27x^3 - \frac{27x^2}{2} + \frac{9x}{4} - \frac{1}{8} =$ $[\frac{(6x-1)^3}{8}]$
- (n) $27x^3 + \frac{27x^2}{2} + \frac{9x}{4} + \frac{1}{8} =$ $[\frac{(6x+1)^3}{8}]$
- (o) $\frac{125x^3}{64} + \frac{75x^2}{16} + \frac{15x}{4} + 1 =$ $[\frac{(5x+4)^3}{64}]$
- (p) $125x^3 - \frac{225x^2}{2} + \frac{135x}{4} - \frac{27}{8} =$ $[\frac{(10x-3)^3}{8}]$
- (q) $-\frac{27x^3}{64} + \frac{27x^2}{16} - \frac{9x}{4} + 1 =$ $[-\frac{(3x-4)^3}{64}]$
- (r) $-\frac{x^3}{8} - \frac{3x^2}{8} - \frac{3x}{8} - \frac{1}{8} =$ $[-\frac{(x+1)^3}{8}]$
- (s) $-\frac{x^3}{8} - \frac{3x^2}{8} - \frac{3x}{8} - \frac{1}{8} =$ $[-\frac{(x+1)^3}{8}]$
- (t) $-\frac{x^3}{64} + \frac{3x^2}{32} - \frac{3x}{16} + \frac{1}{8} =$ $[-\frac{(x-2)^3}{64}]$
- (u) $-\frac{8x^3}{27} - \frac{4x^2}{9} - \frac{2x}{9} - \frac{1}{27} =$ $[-\frac{(2x+1)^3}{27}]$
- (v) $\frac{x^3}{64} + \frac{9x^2}{40} + \frac{27x}{25} + \frac{216}{125} =$ $[\frac{(5x+24)^3}{8000}]$
- (w) $-\frac{x^3}{216} + \frac{5x^2}{72} - \frac{25x}{72} + \frac{125}{216} =$ $[-\frac{(x-5)^3}{216}]$
- (x) $-\frac{x^3}{27} + \frac{2x^2}{5} - \frac{36x}{25} + \frac{216}{125} =$ $[-\frac{(5x-18)^3}{3375}]$
- (y) $-\frac{125x^3}{64} - \frac{15x^2}{8} - \frac{3x}{5} - \frac{8}{125} =$ $[-\frac{(25x+8)^3}{8000}]$
- (z) $-\frac{125x^3}{8} + \frac{45x^2}{2} - \frac{54x}{5} + \frac{216}{125} =$ $[-\frac{(25x-12)^3}{1000}]$

11. Scomponi le seguenti potenze di binomi.

- (a) $x^4 + 8x^3 + 24x^2 + 32x + 16 =$ $[(x+2)^4]$
- (b) $x^4 + 8x^3 + 24x^2 + 32x + 16 =$ $[(x+2)^4]$
- (c) $x^4 - 8x^3 + 24x^2 - 32x + 16 =$ $[(x-2)^4]$
- (d) $x^4 + 8x^3 + 24x^2 + 32x + 16 =$ $[(x+2)^4]$
- (e) $x^4 + 12x^3 + 54x^2 + 108x + 81 =$ $[(x+3)^4]$
- (f) $x^4 - 12x^3 + 54x^2 - 108x + 81 =$ $[(x-3)^4]$
- (g) $x^4 + 12x^3 + 54x^2 + 108x + 81 =$ $[(x+3)^4]$
- (h) $x^4 + 12x^3 + 54x^2 + 108x + 81 =$ $[(x+3)^4]$
- (i) $x^4 + 12x^3 + 54x^2 + 108x + 81 =$ $[(x+3)^4]$
- (j) $x^4 - 16x^3 + 96x^2 - 256x + 256 =$ $[(x-4)^4]$
- (k) $16x^4 + 32x^3 + 24x^2 + 8x + 1 =$ $[(2x+1)^4]$
- (l) $81x^4 - 108x^3 + 54x^2 - 12x + 1 =$ $[(3x-1)^4]$
- (m) $256x^4 - 256x^3 + 96x^2 - 16x + 1 =$ $[(4x-1)^4]$
- (n) $256x^4 + 256x^3 + 96x^2 + 16x + 1 =$ $[(4x+1)^4]$
- (o) $81x^4 - 216x^3 + 216x^2 - 96x + 16 =$ $[(3x-2)^4]$
- (p) $16x^4 - 96x^3 + 216x^2 - 216x + 81 =$ $[(2x-3)^4]$
- (q) $81x^4 + 216x^3 + 216x^2 + 96x + 16 =$ $[(3x+2)^4]$
- (r) $81x^4 + 432x^3 + 864x^2 + 768x + 256 =$ $[(3x+4)^4]$
- (s) $81x^4 - 432x^3 + 864x^2 - 768x + 256 =$ $[(3x-4)^4]$

- (t) $16x^4 - 128x^3 + 384x^2 - 512x + 256 = [16(x-2)^4]$
 (u) $16x^4 + 128x^3 + 384x^2 + 512x + 256 = [16(x+2)^4]$
 (v) $16x^4 + 128x^3 + 384x^2 + 512x + 256 = [16(x+2)^4]$
 (w) $256x^4 - 512x^3 + 384x^2 - 128x + 16 = [16(2x-1)^4]$
 (x) $256x^4 - 512x^3 + 384x^2 - 128x + 16 = [16(2x-1)^4]$
 (y) $256x^4 - 1024x^3 + 1536x^2 - 1024x + 256 = [256(x-1)^4]$
 (z) $256x^4 + 1024x^3 + 1536x^2 + 1024x + 256 = [256(x+1)^4]$

12. Scomponi le seguenti potenze di binomi.

- (a) $x^4 + 4x^3 + 6x^2 + 4x + 1 = [(x+1)^4]$
 (b) $x^4 + 4x^3 + 6x^2 + 4x + 1 = [(x+1)^4]$
 (c) $x^4 - 8x^3 + 24x^2 - 32x + 16 = [(x-2)^4]$
 (d) $16x^4 + 32x^3 + 24x^2 + 8x + 1 = [(2x+1)^4]$
 (e) $81x^4 - 108x^3 + 54x^2 - 12x + 1 = [(3x-1)^4]$
 (f) $256x^4 - 256x^3 + 96x^2 - 16x + 1 = [(4x-1)^4]$
 (g) $16x^4 - 64x^3 + 96x^2 - 64x + 16 = [16(x-1)^4]$
 (h) $256x^4 - 256x^3 + 96x^2 - 16x + 1 = [(4x-1)^4]$
 (i) $256x^4 + 512x^3 + 384x^2 + 128x + 16 = [16(2x+1)^4]$
 (j) $\frac{x^4}{16} - \frac{x^3}{2} + \frac{3x^2}{2} - 2x + 1 = [\frac{(x-2)^4}{16}]$
 (k) $\frac{x^4}{16} + \frac{x^3}{2} + \frac{3x^2}{2} + 2x + 1 = [\frac{(x+2)^4}{16}]$
 (l) $x^4 + x^3 + \frac{3x^2}{8} + \frac{x}{16} + \frac{1}{256} = [\frac{(4x+1)^4}{256}]$
 (m) $\frac{x^4}{16} + \frac{3x^3}{2} + \frac{27x^2}{2} + 54x + 81 = [\frac{(x+6)^4}{16}]$
 (n) $\frac{81x^4}{256} + \frac{27x^3}{16} + \frac{27x^2}{8} + 3x + 1 = [\frac{(3x+4)^4}{256}]$
 (o) $\frac{x^4}{81} + \frac{4x^3}{27} + \frac{2x^2}{3} + \frac{4x}{3} + 1 = [\frac{(x+3)^4}{81}]$
 (p) $x^4 + \frac{8x^3}{3} + \frac{8x^2}{3} + \frac{32x}{27} + \frac{16}{81} = [\frac{(3x+2)^4}{81}]$
 (q) $\frac{16x^4}{81} + \frac{32x^3}{27} + \frac{8x^2}{3} + \frac{8x}{3} + 1 = [\frac{(2x+3)^4}{81}]$
 (r) $\frac{x^4}{16} - \frac{x^3}{4} + \frac{3x^2}{8} - \frac{x}{4} + \frac{1}{16} = [\frac{(x-1)^4}{16}]$
 (s) $x^4 + \frac{16x^3}{3} + \frac{32x^2}{3} + \frac{256x}{27} + \frac{256}{81} = [\frac{(3x+4)^4}{81}]$
 (t) $\frac{256x^4}{81} - \frac{256x^3}{27} + \frac{32x^2}{3} - \frac{16x}{3} + 1 = [\frac{(4x-3)^4}{81}]$
 (u) $\frac{x^4}{16} + \frac{3x^3}{4} + \frac{27x^2}{8} + \frac{27x}{4} + \frac{81}{16} = [\frac{(x+3)^4}{16}]$
 (v) $\frac{x^4}{256} - \frac{x^3}{64} + \frac{3x^2}{128} - \frac{x}{64} + \frac{1}{256} = [\frac{(x-1)^4}{256}]$
 (w) $\frac{x^4}{16} - \frac{3x^3}{4} + \frac{27x^2}{8} - \frac{27x}{4} + \frac{81}{16} = [\frac{(x-3)^4}{16}]$
 (x) $\frac{x^4}{256} - \frac{3x^3}{32} + \frac{27x^2}{32} - \frac{27x}{8} + \frac{81}{16} = [\frac{(x-6)^4}{256}]$
 (y) $256x^4 - \frac{1024x^3}{3} + \frac{512x^2}{3} - \frac{1024x}{27} + \frac{256}{81} = [\frac{256(3x-1)^4}{81}]$
 (z) $\frac{x^4}{256} + \frac{x^3}{12} + \frac{2x^2}{3} + \frac{64x}{27} + \frac{256}{81} = [\frac{(3x+16)^4}{20736}]$

13. Scomponi le seguenti potenze di binomi.

- (a) $x^5 - 5x^4 + 10x^3 - 10x^2 + 5x - 1 = [(x-1)^5]$

- (b) $x^5 + 10x^4 + 40x^3 + 80x^2 + 80x + 32 =$ $[(x+2)^5]$
 (c) $-x^5 + 5x^4 - 10x^3 + 10x^2 - 5x + 1 =$ $[-(x-1)^5]$
 (d) $-x^5 - 5x^4 - 10x^3 - 10x^2 - 5x - 1 =$ $[-(x+1)^5]$
 (e) $-x^5 + 5x^4 - 10x^3 + 10x^2 - 5x + 1 =$ $[-(x-1)^5]$
 (f) $-x^5 - 5x^4 - 10x^3 - 10x^2 - 5x - 1 =$ $[-(x+1)^5]$
 (g) $x^5 - 15x^4 + 90x^3 - 270x^2 + 405x - 243 =$ $[(x-3)^5]$
 (h) $-x^5 + 10x^4 - 40x^3 + 80x^2 - 80x + 32 =$ $[-(x-2)^5]$
 (i) $-x^5 - 15x^4 - 90x^3 - 270x^2 - 405x - 243 =$ $[-(x+3)^5]$
 (j) $243x^5 - 405x^4 + 270x^3 - 90x^2 + 15x - 1 =$ $[(3x-1)^5]$
 (k) $-32x^5 + 80x^4 - 80x^3 + 40x^2 - 10x + 1 =$ $[-(2x-1)^5]$
 (l) $-32x^5 + 80x^4 - 80x^3 + 40x^2 - 10x + 1 =$ $[-(2x-1)^5]$
 (m) $32x^5 - 160x^4 + 320x^3 - 320x^2 + 160x - 32 =$ $[32(x-1)^5]$
 (n) $32x^5 - 160x^4 + 320x^3 - 320x^2 + 160x - 32 =$ $[32(x-1)^5]$
 (o) $-243x^5 - 405x^4 - 270x^3 - 90x^2 - 15x - 1 =$ $[-(3x+1)^5]$
 (p) $243x^5 - 810x^4 + 1080x^3 - 720x^2 + 240x - 32 =$ $[(3x-2)^5]$
 (q) $243x^5 + 810x^4 + 1080x^3 + 720x^2 + 240x + 32 =$ $[(3x+2)^5]$
 (r) $32x^5 - 240x^4 + 720x^3 - 1080x^2 + 810x - 243 =$ $[(2x-3)^5]$
 (s) $-32x^5 - 160x^4 - 320x^3 - 320x^2 - 160x - 32 =$ $[-32(x+1)^5]$
 (t) $-32x^5 + 160x^4 - 320x^3 + 320x^2 - 160x + 32 =$ $[-32(x-1)^5]$
 (u) $-243x^5 - 810x^4 - 1080x^3 - 720x^2 - 240x - 32 =$ $[-(3x+2)^5]$
 (v) $-243x^5 - 810x^4 - 1080x^3 - 720x^2 - 240x - 32 =$ $[-(3x+2)^5]$
 (w) $243x^5 + 1215x^4 + 2430x^3 + 2430x^2 + 1215x + 243 =$ $[243(x+1)^5]$
 (x) $243x^5 - 1215x^4 + 2430x^3 - 2430x^2 + 1215x - 243 =$ $[243(x-1)^5]$
 (y) $-243x^5 - 1215x^4 - 2430x^3 - 2430x^2 - 1215x - 243 =$ $[-243(x+1)^5]$
 (z) $-243x^5 - 1215x^4 - 2430x^3 - 2430x^2 - 1215x - 243 =$ $[-243(x+1)^5]$

14. Scomponi le seguenti potenze di binomi.

- (a) $x^5 - 5x^4 + 10x^3 - 10x^2 + 5x - 1 =$ $[(x-1)^5]$
 (b) $x^5 + 5x^4 + 10x^3 + 10x^2 + 5x + 1 =$ $[(x+1)^5]$
 (c) $x^5 + 5x^4 + 10x^3 + 10x^2 + 5x + 1 =$ $[(x+1)^5]$
 (d) $x^5 + 5x^4 + 10x^3 + 10x^2 + 5x + 1 =$ $[(x+1)^5]$
 (e) $x^5 + 5x^4 + 10x^3 + 10x^2 + 5x + 1 =$ $[(x+1)^5]$
 (f) $-x^5 - 5x^4 - 10x^3 - 10x^2 - 5x - 1 =$ $[-(x+1)^5]$
 (g) $-x^5 + 10x^4 - 40x^3 + 80x^2 - 80x + 32 =$ $[-(x-2)^5]$
 (h) $-x^5 - 15x^4 - 90x^3 - 270x^2 - 405x - 243 =$ $[-(x+3)^5]$
 (i) $-x^5 + 15x^4 - 90x^3 + 270x^2 - 405x + 243 =$ $[-(x-3)^5]$
 (j) $-32x^5 - 80x^4 - 80x^3 - 40x^2 - 10x - 1 =$ $[-(2x+1)^5]$
 (k) $-32x^5 + 80x^4 - 80x^3 + 40x^2 - 10x + 1 =$ $[-(2x-1)^5]$
 (l) $-243x^5 + 405x^4 - 270x^3 + 90x^2 - 15x + 1 =$ $[-(3x-1)^5]$
 (m) $-32x^5 + 240x^4 - 720x^3 + 1080x^2 - 810x + 243 =$ $[-(2x-3)^5]$

- (n) $-243x^5 - 810x^4 - 1080x^3 - 720x^2 - 240x - 32 =$ $[-(3x+2)^5]$
 (o) $32x^5 - 120x^4 + 180x^3 - 135x^2 + \frac{405x}{8} - \frac{243}{32} =$ $[\frac{(4x-3)^5}{32}]$
 (p) $-32x^5 + 120x^4 - 180x^3 + 135x^2 - \frac{405x}{8} + \frac{243}{32} =$ $[-\frac{(4x-3)^5}{32}]$
 (q) $x^5 - \frac{5x^4}{3} + \frac{10x^3}{9} - \frac{10x^2}{27} + \frac{5x}{81} - \frac{1}{243} =$ $[\frac{(3x-1)^5}{243}]$
 (r) $-x^5 - \frac{5x^4}{3} - \frac{10x^3}{9} - \frac{10x^2}{27} - \frac{5x}{81} - \frac{1}{243} =$ $[-\frac{(3x+1)^5}{243}]$
 (s) $-\frac{x^5}{243} - \frac{10x^4}{81} - \frac{40x^3}{27} - \frac{80x^2}{9} - \frac{80x}{3} - 32 =$ $[-\frac{(x+6)^5}{243}]$
 (t) $\frac{32x^5}{243} + \frac{80x^4}{81} + \frac{80x^3}{27} + \frac{40x^2}{9} + \frac{10x}{3} + 1 =$ $[\frac{(2x+3)^5}{243}]$
 (u) $\frac{32x^5}{243} + \frac{80x^4}{81} + \frac{80x^3}{27} + \frac{40x^2}{9} + \frac{10x}{3} + 1 =$ $[\frac{(2x+3)^5}{243}]$
 (v) $-\frac{x^5}{32} + \frac{15x^4}{16} - \frac{45x^3}{4} + \frac{135x^2}{2} - \frac{405x}{2} + 243 =$ $[-\frac{(x-6)^5}{32}]$
 (w) $\frac{32x^5}{243} + \frac{80x^4}{81} + \frac{80x^3}{27} + \frac{40x^2}{9} + \frac{10x}{3} + 1 =$ $[\frac{(2x+3)^5}{243}]$
 (x) $-243x^5 + \frac{405x^4}{2} - \frac{135x^3}{2} + \frac{45x^2}{4} - \frac{15x}{16} + \frac{1}{32} =$ $[-\frac{(6x-1)^5}{32}]$
 (y) $-\frac{x^5}{243} - \frac{5x^4}{162} - \frac{5x^3}{54} - \frac{5x^2}{36} - \frac{5x}{48} - \frac{1}{32} =$ $[-\frac{(2x+3)^5}{776}]$
 (z) $-\frac{x^5}{243} - \frac{5x^4}{162} - \frac{5x^3}{54} - \frac{5x^2}{36} - \frac{5x}{48} - \frac{1}{32} =$ $[-\frac{(2x+3)^5}{776}]$

15. Scomponi i seguenti polinomi con il raccoglimento a fattore comune.

- (a) $-10x^8 + 10x^6 + 4x^5 =$ $[-2x^5(5x^3 - 5x - 2)]$
 (b) $-32x^5 + 28x^3 + 44x^2 =$ $[-4x^2(8x^3 - 7x - 11)]$
 (c) $-20x^5 + 50x^4 + 55x^2 - 45x =$ $[-5x(4x^4 - 10x^3 - 11x + 9)]$
 (d) $-24x^9 + 14x^8 - 4x^6 + 4x^5 =$ $[-2x^5(12x^4 - 7x^3 + 2x - 2)]$
 (e) $5x^5 + 30x^4 - 10x^3 - 25x^2 + 45x =$ $[5x(x^4 + 6x^3 - 2x^2 - 5x + 9)]$
 (f) $x^8 + 3x^7 + 7x^6 + 3x^5 - 7x^4 =$ $[x^4(x^4 + 3x^3 + 7x^2 + 3x - 7)]$
 (g) $6x^5 + 16x^4 + 14x^3 - 10x^2 + 2x =$ $[2x(3x^4 + 8x^3 + 7x^2 - 5x + 1)]$
 (h) $20x^5 - 25x^4 + 30x^3 - 30x^2 + 45x =$ $[5x(4x^4 - 5x^3 + 6x^2 - 6x + 9)]$
 (i) $-2x^5 + 12x^4 - 4x^3 + 20x^2 + 18x =$ $[-2x(x^4 - 6x^3 + 2x^2 - 10x - 9)]$
 (j) $33x^5 + 36x^4 - 15x^3 - 12x^2 + 24x =$ $[3x(11x^4 + 12x^3 - 5x^2 - 4x + 8)]$
 (k) $-30x^5 - 66x^4 - 72x^3 + 24x^2 - 6x =$ $[-6x(5x^4 + 11x^3 + 12x^2 - 4x + 1)]$
 (l) $-12x^5 - 66x^4 + 24x^3 + 30x^2 + 30x =$ $[-6x(2x^4 + 11x^3 - 4x^2 - 5x - 5)]$
 (m) $-48x^5 - 66x^4 + 48x^3 + 18x^2 + 24x =$ $[-6x(8x^4 + 11x^3 - 8x^2 - 3x - 4)]$
 (n) $-16x^5 - 4x^4 - 24x^3 - 14x^2 + 20x =$ $[-2x(8x^4 + 2x^3 + 12x^2 + 7x - 10)]$
 (o) $11x^{10} - 2x^9 + 3x^8 + 4x^7 + 10x^6 =$ $[x^6(11x^4 - 2x^3 + 3x^2 + 4x + 10)]$
 (p) $24x^6 + 33x^5 + 24x^4 - 3x^3 + 27x^2 =$ $[3x^2(8x^4 + 11x^3 + 8x^2 - x + 9)]$
 (q) $20x^9 + 5x^8 + 50x^7 + 55x^6 + 30x^5 =$ $[5x^5(4x^4 + x^3 + 10x^2 + 11x + 6)]$
 (r) $-20x^8 + 5x^7 + 55x^6 + 30x^5 + 5x^4 =$ $[-5x^4(4x^4 - x^3 - 11x^2 - 6x - 1)]$
 (s) $-25x^7 - 45x^6 - 40x^5 - 30x^4 - 30x^3 =$ $[-5x^3(5x^4 + 9x^3 + 8x^2 + 6x + 6)]$
 (t) $-12x^6 - 48x^5 + 28x^4 - 44x^3 - 8x^2 =$ $[-4x^2(3x^4 + 12x^3 - 7x^2 + 11x + 2)]$
 (u) $-32x^9 - 28x^8 - 16x^7 - 28x^6 - 48x^5 =$ $[-4x^5(8x^4 + 7x^3 + 4x^2 + 7x + 12)]$
 (v) $-72x^6 + 42x^5 - 36x^4 - 24x^3 + 12x^2 =$ $[-6x^2(12x^4 - 7x^3 + 6x^2 + 4x - 2)]$
 (w) $35x^6 - 10x^5 - 20x^4 + 5x^3 - 10x^2 =$ $[5x^2(x - 1)(7x^3 + 5x^2 + x + 2)]$

- (x) $-60x^8 + 45x^7 - 50x^6 - 30x^5 - 40x^4 =$
 (y) $-16x^5 + 44x^4 - 48x^3 - 28x^2 + 48x =$
 (z) $-12x^6 - 28x^5 + 44x^4 - 48x^3 - 48x^2 =$

$$[-5x^4(12x^4 - 9x^3 + 10x^2 + 6x + 8)] \\ [-4x(x-1)(4x^3 - 7x^2 + 5x + 12)] \\ [-4x^2(3x^4 + 7x^3 - 11x^2 + 12x + 12)]$$

16. Scomponi i seguenti polinomi con il raccoglimento a fattore comune.

- (a) $5x^5 - 6x^4 + 11x^3 - 11x^2 - x =$
 (b) $8x^9 - 12x^8 + 32x^7 - 20x^6 + 8x^5 =$
 (c) $-4x^9 + 16x^8 - 2x^7 + 8x^6 - 14x^5 =$
 (d) $8x^6 - 4x^5 - 16x^4 - 14x^3 + 24x^2 =$
 (e) $21x^6 + 15x^5 - 27x^4 - 18x^3 - 33x^2 =$
 (f) $-10x^9 - 5x^8 + 7x^7 + 5x^6 + 3x^5 =$
 (g) $-6x^7 + 48x^6 - 6x^5 - 48x^4 + 12x^3 =$
 (h) $\frac{12x^{10}}{5} - \frac{x^9}{5} + \frac{9x^7}{5} - \frac{3x^6}{5} =$
 (i) $\frac{3x^5}{2} + 9x^4 + 6x^3 + \frac{3x^2}{2} + \frac{27x}{2} =$
 (j) $-12x^7 - \frac{40x^6}{3} - 12x^5 + 12x^4 - 8x^3 =$
 (k) $-3x^5 + 4x^4 + \frac{8x^3}{3} - \frac{x^2}{3} - \frac{7x}{3} =$
 (l) $-\frac{8x^5}{3} + \frac{11x^4}{3} + \frac{11x^3}{3} + 2x^2 + x =$
 (m) $-\frac{24x^9}{5} + 12x^8 - \frac{12x^7}{5} - 12x^6 - 6x^5 =$
 (n) $-x^6 - 4x^5 - \frac{8x^4}{3} + \frac{5x^3}{3} - \frac{4x^2}{3} =$
 (o) $4x^6 + \frac{16x^5}{3} + \frac{2x^4}{3} - \frac{14x^3}{3} + 8x^2 =$
 (p) $-12x^5 + \frac{9x^4}{2} - 15x^3 + \frac{33x^2}{2} - \frac{9x}{2} =$
 (q) $3x^9 - \frac{36x^8}{5} + \frac{18x^7}{5} + 6x^6 + \frac{9x^5}{5} =$
 (r) $5x^9 + \frac{15x^8}{2} + \frac{15x^7}{4} - \frac{25x^6}{2} + 15x^5 =$
 (s) $-\frac{5x^{10}}{3} - \frac{8x^9}{3} - x^8 - \frac{11x^7}{3} - \frac{x^6}{3} =$
 (t) $-\frac{4x^{10}}{3} + \frac{5x^9}{3} + 2x^8 + \frac{5x^7}{3} + \frac{2x^6}{3} =$
 (u) $-\frac{5x^6}{3} + \frac{10x^5}{3} - \frac{10x^4}{3} - \frac{25x^3}{3} + 5x^2 =$
 (v) $15x^9 - \frac{25x^8}{3} - \frac{35x^7}{3} + \frac{35x^6}{3} + \frac{55x^5}{3} =$
 (w) $-18x^5 + \frac{21x^4}{2} + \frac{33x^3}{2} - \frac{9x^2}{2} - \frac{9x}{2} =$
 (x) $\frac{16x^6}{5} + \frac{36x^5}{5} + \frac{8x^4}{5} - \frac{44x^3}{5} + \frac{8x^2}{5} =$
 (y) $\frac{x^{10}}{5} - \frac{8x^9}{5} + \frac{2x^8}{5} - \frac{6x^7}{5} + \frac{11x^6}{5} =$
 (z) $-\frac{3x^{10}}{4} + \frac{5x^9}{2} + \frac{11x^8}{4} + \frac{5x^7}{2} - \frac{5x^6}{4} =$

$$[x(5x^4 - 6x^3 + 11x^2 - 11x - 1)] \\ [4x^5(2x^4 - 3x^3 + 8x^2 - 5x + 2)] \\ [-2x^5(2x^4 - 8x^3 + x^2 - 4x + 7)] \\ [2x^2(4x^4 - 2x^3 - 8x^2 - 7x + 12)] \\ [3x^2(7x^4 + 5x^3 - 9x^2 - 6x - 11)] \\ [-x^5(x-1)(x+1)(10x^2 + 5x + 3)] \\ [-6x^3(x-1)(x+1)(x^2 - 8x + 2)] \\ [\frac{x^6(12x^4 - x^3 + 9x - 3)}{5}] \\ [\frac{3x(x^4 + 6x^3 + 4x^2 + x + 9)}{2}] \\ [-\frac{4x^3(9x^4 + 10x^3 + 9x^2 - 9x + 6)}{3}] \\ [-\frac{x(9x^4 - 12x^3 - 8x^2 + x + 7)}{3}] \\ [-\frac{x(8x^4 - 11x^3 - 11x^2 - 6x - 3)}{3}] \\ [-\frac{6x^5(4x^4 - 10x^3 + 2x^2 + 10x + 5)}{5}] \\ [-\frac{x^2(3x^4 + 12x^3 + 8x^2 - 5x + 4)}{3}] \\ [\frac{2x^2(6x^4 + 8x^3 + x^2 - 7x + 12)}{3}] \\ [-\frac{3x(8x^4 - 3x^3 + 10x^2 - 11x + 3)}{2}] \\ [\frac{3x^5(5x^4 - 12x^3 + 6x^2 + 10x + 3)}{5}] \\ [\frac{5x^5(4x^4 + 6x^3 + 3x^2 - 10x + 12)}{4}] \\ [-\frac{x^6(5x^4 + 8x^3 + 3x^2 + 11x + 1)}{3}] \\ [-\frac{x^6(4x^4 - 5x^3 - 6x^2 - 5x - 2)}{3}] \\ [-\frac{5x^2(x^4 - 2x^3 + 2x^2 + 5x - 3)}{3}] \\ [\frac{5x^5(9x^4 - 5x^3 - 7x^2 + 7x + 11)}{3}] \\ [-\frac{3x(x-1)(12x^3 + 5x^2 - 6x - 3)}{2}] \\ [\frac{4x^2(4x^4 + 9x^3 + 2x^2 - 11x + 2)}{5}] \\ [\frac{x^6(x-1)(x^3 - 7x^2 - 5x - 11)}{5}] \\ [-\frac{x^6(3x^4 - 10x^3 - 11x^2 - 10x + 5)}{4}]$$

17. Scomponi i seguenti polinomi.

- (a) $x^3 + x^2 + x + 1 =$
 (b) $x^3 - 5x^2 + x - 5 =$
 (c) $x^3 - 4x^2 + x - 4 =$

$$[(x+1)(x^2 + 1)] \\ [(x-5)(x^2 + 1)] \\ [(x-4)(x^2 + 1)]$$

- (d) $-x^3 - 8x^2 - x - 8 =$ $[-(x+8)(x^2 + 1)]$
 (e) $9x^3 + 4x^2 + 9x + 4 =$ $[(9x+4)(x^2 + 1)]$
 (f) $9x^3 + 7x^2 + 9x + 7 =$ $[(9x+7)(x^2 + 1)]$
 (g) $8x^3 - 8x^2 + 8x - 8 =$ $[8(x-1)(x^2 + 1)]$
 (h) $9x^3 - 5x^2 + 9x - 5 =$ $[(9x-5)(x^2 + 1)]$
 (i) $2x^3 + 5x^2 + 2x + 5 =$ $[(2x+5)(x^2 + 1)]$
 (j) $4x^3 - 4x^2 + 4x - 4 =$ $[4(x-1)(x^2 + 1)]$
 (k) $-6x^3 - x^2 - 6x - 1 =$ $[-(6x+1)(x^2 + 1)]$
 (l) $6x^3 - 4x^2 + 6x - 4 =$ $[2(3x-2)(x^2 + 1)]$
 (m) $10x^3 - 7x^2 + 10x - 7 =$ $[(10x-7)(x^2 + 1)]$
 (n) $6x^3 + 11x^2 + 6x + 11 =$ $[(6x+11)(x^2 + 1)]$
 (o) $12x^3 + 9x^2 + 12x + 9 =$ $[3(4x+3)(x^2 + 1)]$
 (p) $-5x^3 - 3x^2 - 5x - 3 =$ $[-(5x+3)(x^2 + 1)]$
 (q) $10x^3 - 2x^2 + 10x - 2 =$ $[2(5x-1)(x^2 + 1)]$
 (r) $10x^3 - 10x^2 + 10x - 10 =$ $[10(x-1)(x^2 + 1)]$
 (s) $-6x^3 - 9x^2 - 6x - 9 =$ $[-3(2x+3)(x^2 + 1)]$
 (t) $-6x^3 + 12x^2 - 6x + 12 =$ $[-6(x-2)(x^2 + 1)]$
 (u) $-7x^3 + 11x^2 - 7x + 11 =$ $[-(7x-11)(x^2 + 1)]$
 (v) $-11x^3 + 4x^2 - 11x + 4 =$ $[-(11x-4)(x^2 + 1)]$
 (w) $-12x^3 + 7x^2 - 12x + 7 =$ $[-(12x-7)(x^2 + 1)]$
 (x) $-8x^3 - 11x^2 - 8x - 11 =$ $[-(8x+11)(x^2 + 1)]$
 (y) $-6x^3 + 10x^2 - 6x + 10 =$ $[-2(3x-5)(x^2 + 1)]$
 (z) $-10x^3 + 12x^2 - 10x + 12 =$ $[-2(5x-6)(x^2 + 1)]$

18. Scomponi i seguenti polinomi.

- (a) $-x^3 + 2x^2 - x + 2 =$ $[-(x-2)(x^2 + 1)]$
 (b) $-2x^3 - 3x^2 - 2x - 3 =$ $[-(2x+3)(x^2 + 1)]$
 (c) $\frac{x^3}{4} - 9x^2 + \frac{x}{4} - 9 =$ $[\frac{(x-36)(x^2+1)}{4}]$
 (d) $x^3 + \frac{2x^2}{3} + x + \frac{2}{3} =$ $[\frac{(3x+2)(x^2+1)}{3}]$
 (e) $-x^3 + \frac{11x^2}{3} - x + \frac{11}{3} =$ $[-\frac{(3x-11)(x^2+1)}{3}]$
 (f) $2x^3 - \frac{11x^2}{9} + 2x - \frac{11}{9} =$ $[\frac{(18x-11)(x^2+1)}{9}]$
 (g) $-3x^3 + \frac{7x^2}{3} - 3x + \frac{7}{3} =$ $[-\frac{(9x-7)(x^2+1)}{3}]$
 (h) $-\frac{11x^3}{7} + x^2 - \frac{11x}{7} + 1 =$ $[-\frac{(11x-7)(x^2+1)}{7}]$
 (i) $-\frac{3x^3}{4} + 9x^2 - \frac{3x}{4} + 9 =$ $[-\frac{3(x-12)(x^2+1)}{4}]$
 (j) $-\frac{x^3}{3} + \frac{3x^2}{2} - \frac{x}{3} + \frac{3}{2} =$ $[-\frac{(2x-9)(x^2+1)}{6}]$
 (k) $\frac{5x^3}{6} + \frac{3x^2}{4} + \frac{5x}{6} + \frac{3}{4} =$ $[\frac{(10x+9)(x^2+1)}{12}]$
 (l) $\frac{7x^3}{3} + \frac{7x^2}{5} + \frac{7x}{3} + \frac{7}{5} =$ $[\frac{7(5x+3)(x^2+1)}{15}]$
 (m) $\frac{4x^3}{7} + \frac{4x^2}{5} + \frac{4x}{7} + \frac{4}{5} =$ $[\frac{4(5x+7)(x^2+1)}{35}]$

- (n) $\frac{3x^3}{5} - \frac{9x^2}{8} + \frac{3x}{5} - \frac{9}{8} =$ $[\frac{3(8x-15)(x^2+1)}{40}]$
- (o) $-\frac{7x^3}{4} - \frac{3x^2}{4} - \frac{7x}{4} - \frac{3}{4} =$ $[-\frac{(7x+3)(x^2+1)}{4}]$
- (p) $\frac{5x^3}{3} - \frac{7x^2}{12} + \frac{5x}{3} - \frac{7}{12} =$ $[\frac{(20x-7)(x^2+1)}{12}]$
- (q) $\frac{6x^3}{5} - \frac{11x^2}{9} + \frac{6x}{5} - \frac{11}{9} =$ $[\frac{(54x-55)(x^2+1)}{45}]$
- (r) $-\frac{5x^3}{2} - \frac{4x^2}{9} - \frac{5x}{2} - \frac{4}{9} =$ $[-\frac{(45x+8)(x^2+1)}{18}]$
- (s) $-\frac{3x^3}{4} + \frac{8x^2}{5} - \frac{3x}{4} + \frac{8}{5} =$ $[-\frac{(15x-32)(x^2+1)}{20}]$
- (t) $-\frac{3x^3}{2} - \frac{8x^2}{7} - \frac{3x}{2} - \frac{8}{7} =$ $[-\frac{(21x+16)(x^2+1)}{14}]$
- (u) $-\frac{4x^3}{9} + \frac{7x^2}{8} - \frac{4x}{9} + \frac{7}{8} =$ $[-\frac{(32x-63)(x^2+1)}{72}]$
- (v) $-\frac{4x^3}{5} + \frac{9x^2}{4} - \frac{4x}{5} + \frac{9}{4} =$ $[-\frac{(16x-45)(x^2+1)}{20}]$
- (w) $-\frac{3x^3}{5} - \frac{2x^2}{9} - \frac{3x}{5} - \frac{2}{9} =$ $[-\frac{(27x+10)(x^2+1)}{45}]$
- (x) $\frac{11x^3}{5} - \frac{7x^2}{12} + \frac{11x}{5} - \frac{7}{12} =$ $[\frac{(132x-35)(x^2+1)}{60}]$
- (y) $-\frac{2x^3}{11} + \frac{11x^2}{9} - \frac{2x}{11} + \frac{11}{9} =$ $[-\frac{(18x-121)(x^2+1)}{99}]$
- (z) $-\frac{12x^3}{11} + \frac{3x^2}{4} - \frac{12x}{11} + \frac{3}{4} =$ $[-\frac{3(16x-11)(x^2+1)}{44}]$

19. Scomponi i seguenti polinomi usando la regola di Ruffini.

- (a) $x^2 - 12x + 36 =$ $[(x-6)^2]$
- (b) $x^2 - 10x + 24 =$ $[(x-6)(x-4)]$
- (c) $-x^2 + x + 6 =$ $[-(x-3)(x+2)]$
- (d) $-x^2 - x + 12 =$ $[-(x-3)(x+4)]$
- (e) $-x^2 + 4x + 12 =$ $[-(x-6)(x+2)]$
- (f) $2x^2 + 13x + 6 =$ $[(x+6)(2x+1)]$
- (g) $3x^2 - 11x - 4 =$ $[(x-4)(3x+1)]$
- (h) $3x^2 + 10x - 8 =$ $[(x+4)(3x-2)]$
- (i) $-x^2 + 7x - 12 =$ $[-(x-4)(x-3)]$
- (j) $2x^2 - 11x - 6 =$ $[(x-6)(2x+1)]$
- (k) $3x^3 - 9x + 6 =$ $[3(x-1)^2(x+2)]$
- (l) $2x^3 + x^2 - 3 =$ $[(x-1)(2x^2+3x+3)]$
- (m) $-x^3 + x^2 + 8x - 12 =$ $[-(x-2)^2(x+3)]$
- (n) $x^3 - 8x^2 + 10x + 4 =$ $[(x-2)(x^2 - 6x - 2)]$
- (o) $x^3 + 2x^2 - 27x - 18 =$ $[(x+6)(x^2 - 4x - 3)]$
- (p) $-x^3 + 19x + 30 =$ $[-(x-5)(x+2)(x+3)]$
- (q) $3x^3 - 16x^2 + 11x + 20 =$ $[(x-4)(3x^2 - 4x - 5)]$
- (r) $2x^4 + 3x^3 - 2x^2 + 3 =$ $[(x+1)(2x^3 + x^2 - 3x + 3)]$
- (s) $x^4 - 7x^3 + 5x^2 - x + 2 =$ $[(x-1)(x^3 - 6x^2 - x - 2)]$
- (t) $2x^4 + 9x^3 + 5x^2 + 8x + 16 =$ $[(x+4)(2x^3 + x^2 + x + 4)]$
- (u) $2x^4 - 2x^3 - x^2 - 9x + 6 =$ $[(x-2)(2x^3 + 2x^2 + 3x - 3)]$
- (v) $x^4 - 9x^3 + 23x^2 - 14x + 8 =$ $[(x-4)(x^3 - 5x^2 + 3x - 2)]$

- (w) $x^4 + 3x^3 - 14x^2 - 23x - 15 =$ $[(x+5)(x^3 - 2x^2 - 4x - 3)]$
 (x) $3x^4 - 11x^3 + x^2 + 13x + 6 =$ $[(x-3)(3x^3 - 2x^2 - 5x - 2)]$
 (y) $2x^4 - 8x^3 + 9x^2 - 7x - 6 =$ $[(x-3)(2x^3 - 2x^2 + 3x + 2)]$
 (z) $-x^4 - 6x^3 - 6x^2 + 3x - 2 =$ $[-(x+2)(x^3 + 4x^2 - 2x + 1)]$

20. Scomponi i seguenti polinomi.

- (a) $36x^4 - 48x^3 - 32x^2 + 32x + 16 =$ $[4(3x^2 - 2x - 2)^2]$
 (b) $\frac{9x^4}{4} - x^3 - \frac{53x^2}{9} + \frac{4x}{3} + 4 =$ $[\frac{(9x^2 - 2x - 12)^2}{36}]$
 (c) $25x^4 + 60x^3 - 14x^2 - 60x + 25 =$ $[(5x^2 + 6x - 5)^2]$
 (d) $\frac{x^4}{36} - \frac{x^3}{3} + 3x^2 - 12x + 36 =$ $[\frac{(x^2 - 6x + 36)^2}{36}]$
 (e) $-243x^5 + 1215x^4 - 2430x^3 + 2430x^2 - 1215x + 243 =$ $[-243(x-1)^5]$
 (f) $-48x^7 - 36x^6 + 32x^4 + 4x^3 =$ $[-4x^3(12x^4 + 9x^3 - 8x - 1)]$
 (g) $\frac{64x^2}{81} - \frac{4}{9} =$ $[\frac{4(4x-3)(4x+3)}{81}]$
 (h) $x^2 - 17x + 60 =$ $[(x-12)(x-5)]$
 (i) $36x^4 - 72x^3 + 36x + 9 =$ $[9(2x^2 - 2x - 1)^2]$
 (j) $12x^3 + 12x^2 + 12x + 12 =$ $[12(x+1)(x^2 + 1)]$
 (k) $-125x^3 + 225x^2 - 135x + 27 =$ $[-(5x-3)^3]$
 (l) $\frac{5x^3}{3} + \frac{x^2}{10} + \frac{5x}{3} + \frac{1}{10} =$ $[\frac{(50x+3)(x^2+1)}{30}]$
 (m) $-10x^3 + 10x^2 - 10x + 10 =$ $[-10(x-1)(x^2 + 1)]$
 (n) $42x^9 + 54x^8 - 18x^7 - 18x^6 + 54x^5 =$ $[6x^5(7x^4 + 9x^3 - 3x^2 - 3x + 9)]$
 (o) $4x^2 - \frac{1}{16} =$ $[\frac{(8x-1)(8x+1)}{16}]$
 (p) $25x^4 - 50x^3 - 25x^2 + 50x + 25 =$ $[25(x^2 - x - 1)^2]$
 (q) $-8x^3 - 12x^2 - 6x - 1 =$ $[-(2x+1)^3]$
 (r) $x^2 - 3x - 70 =$ $[(x-10)(x+7)]$
 (s) $125x^3 - 45x^2 + \frac{27x}{5} - \frac{27}{125} =$ $[\frac{(25x-3)^3}{125}]$
 (t) $\frac{x^3}{4} - \frac{9x^2}{10} + \frac{x}{4} - \frac{9}{10} =$ $[\frac{(5x-18)(x^2+1)}{20}]$
 (u) $81x^2 - 100 =$ $[(9x-10)(9x+10)]$
 (v) $16x^4 - 40x^3 - 15x^2 + 50x + 25 =$ $[(4x^2 - 5x - 5)^2]$
 (w) $x^5 - 10x^4 + 40x^3 - 80x^2 + 80x - 32 =$ $[(x-2)^5]$
 (x) $x^8 + 8x^7 - 9x^6 + 12x^5 - 11x^4 =$ $[x^4(x^4 + 8x^3 - 9x^2 + 12x - 11)]$
 (y) $-32x^5 - 160x^4 - 320x^3 - 320x^2 - 160x - 32 =$ $[-32(x+1)^5]$
 (z) $x^2 + \frac{2x}{3} - \frac{1}{3} =$ $[\frac{(x+1)(3x-1)}{3}]$