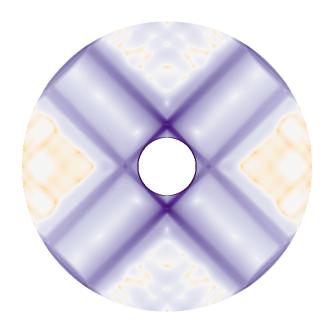
XSHELLS 1.3 : User Manual

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Chapter 1

Getting Started

1.1 Description

XSHELLS is yet another code simulating incompressible fluids in a spherical cavity. In addition to the Navier-Stokes equation with an optional Coriolis force, it can also time-step the coupled induction equation for MHD (with imposed magnetic field or in a dynamo regime), as well as the temperature (or codensity) equation in the Boussineq framework.

XSHELLS uses finite differences (second order) in the radial direction and spherical harmonic decomposition (pseudo-spectral). The time-stepping uses semi-implicit Crank-Nicolson scheme for the diffusive terms, while the non-linear terms can be handled either by an Adams-Bashforth or a Predictor-Corrector scheme (both second order in time).

XSHELLS is written in C++ and designed for speed. It uses the blazingly fast spherical harmonic transform library SHTns, as well as hybrid parallelization using OpenMP and/or MPI. This allows it to run efficiently on your laptop or on parallel supercomputers. A post-processing program is provided to extract useful data and export fields to matlab/octave, python/matplotlib or paraview.

XSHELLS is free software, distributed under the CeCILL Licence (compatible with GNU GPL): everybody is free to use, modify and contribute to the code.

1.2 Requirements

The following items are required:

- a Unix like system (like linux),
- a C++ compiler,
- the FFTW library, or the intel MKL library.
- the SHTns library,

The following items are recommended, but not mandatory:

- a C++ compiler with OpenMP support,
- an MPI library (with thread support),
- the HDF5 library for post-processing and interfacing with paraview,
- Python 3, with NumPy and matplotlib (Python 2.7 should also work),
- a processor supporting the AVX instruction set.
- Gnuplot, for real-time plotting.

1.3 Installation

FFTW and SHTns must be installed first. FFTW comes already installed on many systems, but in order to get high performance, you should install it yourself, and use the optimization options that correspond to your machine (e.g. --enable-avx). Please refer to the FFTW installation guide.

Note that it is possible to use the intel MKL library instead of FFTW. To do so, you must configure both SHTns and XSHELLS with the --enable-mkl option.

To install SHTns, get the latest version of SHTns, extract it and run:

```
./configure
make
make install
```

This will install the serial version (without OpenMP) of SHTns, which is the one required for XSHELLS. If you do not have administrator privileges, you can use ./configure --prefix=\$HOME to install it in your home directory. To choose another compiler than the default one, use ./configure CC=my-c-compiler.

To install XSHELLS, grab the XSHELLS archive, extract it, and then run

```
./configure
```

to automatically configure XSHELLS for your machine. If you have used the --prefix option when installing SHTns, you should pass the same one to configure for XSHELLS. Type ./configure --help to see available options, among which --disable-openmp and --disable-mpi.

Before compiling, you need to setup the xshells.hpp configuration file (see next section).

1.4 Configuration files

There are two configuration files:

- xshells.hpp is read by the compiler (compile-time options), and modifying it requires to recompile the program. The corresponding options are detailed in section 2.2.
- xshells.par is read by the program at startup (runtime options) and modifying it does not require to recompile the program. This file is detailed in section 2.1.

See chapter 2 for more details. Example configuration files can be found in the **problems** directory.

Before compiling, copy the configurations files that correspond most closely to your problem. For example, the geodynamo benchmark:

```
cp problems/geodynamo/xshells.par .
cp problems/geodynamo/xshells.hpp .
and then edit them to adjust the parameters (see sections 2.2 and 2.1).
```

1.5 Compiling and Running

When you have properly set the xshells.hpp and xshells.par files, you can compile and run in different flavours:

Parallel execution using OpenMP with as many threads as processors:

```
make xsbig
./xsbig
```

Parallel execution using OpenMP with (e.g.) 4 threads:

```
make xsbig
OMP_NUM_THREADS=4 ./xsbig
```

Parallel execution using MPI with (e.g.) 4 processes:

```
make xsbig_mpi
mpirun -n 4 ./xsbig_mpi
```

Parallel execution using OpenMP and MPI simultaneously (hybrid parallelization), with (e.g.) 2 processes and 4 threads per process:

```
make xsbig_hyb
OMP_NUM_THREADS=4 mpirun -n 2 ./xsbig_hyb
```

Parallel execution using MPI in the radial direction and OpenMP in the angular direction, with (e.g.) 16 processes and 8 threads per process:

```
make xsbig_hyb2
OMP_NUM_THREADS=8 mpirun -n 16 ./xsbig_hyb2
```

1.6 Outputs

All output files are suffixed by the job name as file extension, denoted job in the following. The various output files are:

- xshells.par.job: a copy of the input parameter file xshells.par, for future reference.
- xshells.hpp.job: a stripped-out version of the file xshells.hpp that was used during compilation, for future reference.
- energy.job: a record of energies and other custom diagnostics. Each line of this text file is an iteration.
- fieldX0.job: the imposed (constant) field X, if any.
- fieldX_####.job: the field X at iteration number ####, if parameter movie was set to a non-zero value in xshells.par.
- fieldXavg_###.job: the field X averaged between previous iteration and iteration number ####, if parameter movie was set to 2 in xshells.par.
- fieldX.job: the last full backup of field X, or field X at the end of the simulation. Used when restarting a job.

All field files are binary format files storing the spherical harmonic coefficients of the field. To produce plots and visualizations, they can be post-processed using the xspp program (see chapter 3).

1.7 Limitations and advice for parallel execution

The parallelization of XSHELLS is done by domain decomposition in the radial direction only, using MPI. In addition to this domain decomposition, shared memory parallelism is implemented using OpenMP. There are four variants of the code that differ in the way OpenMP is used:

- xsbig uses only OpenMP in the radial direction (no MPI). It can only run on a single node, but does not need an MPI library. This is good for a general purpose desktop or laptop computer, but also on NUMA nodes (although some MPI may lead to better performance).
- xsbig_mpi uses only MPI in the radial direction (no OpenMP). This is good for medium sized problems, running on small clusters.

- xsbig_hyb uses both MPI and OpenMP in the radial direction, to reduce the number of MPI processes and memory usage. As a consequence, it is more efficient to use a number of radial shells that is a multiple of the number of computing cores. This parallelization strategy cannot go beyond 1 thread per radial shell, but is computationally very efficient.
- xsbig_hyb2 uses MPI in the radial direction and OpenMP within a radial shell. This reduces further the memory footprint. It is slightly slower than the previous mode (xsbig_hyb), but allows to address more computing cores. It is highly recommended to use a number of radial shells that is a multiple of the number of nodes. This mode cannot go beyond 1 MPI process per radial shell, but intra-node shared memory parallelism allows to use all cores of a single node within each process. Note also that the SHTns library compiled with OpenMP is needed.

In any case, the number of MPI processes cannot exceed the total number of radial shells. It is often more efficient to use a small number of MPI processes per node (1 to 4) and use OpenMP to have a total number of threads equal to the number of cores.

Because there is no automatic load balancing, some situations where the same amount of work is not required for each radial shell will result in suboptimal scaling when the number of MPI processes is increased. Such situations include (i) solid conducting shells (e.g. a conducting inner core) and (ii) variable spherical harmonic degree truncation (e.g. in a full-sphere problem). In these cases, especially the latter, use pure OpenMP or minimize the number of MPI processes.

Using MPI executables (including hybrid MPI+OpenMP) is thus optimal only if the following conditions are both met:

- all fields span the same radial domain (no conducting solid shells);
- the radial domain does not include the center r = 0 (and XS_VAR_LTR is not used, see section 2.2.5).

In such cases, XSHELLS should scale very well up to the limit of 1 thread per radial shell, and even beyond with the in-shell OpenMP mode of xsbig_hyb2 (see scaling example in Figure 1.1).

1.8 Citing

If you use XSHELLS for research work, you should cite the SHTns paper (because the high performance of XSHELLS is mostly due to the blazingly fast spherical harmonic transform provided by SHTns):

N. Schaeffer, Efficient Spherical Harmonic Transforms aimed at pseudo-spectral numerical simulations, Geochem. Geophys. Geosyst. 14, 751-758, doi:10.1002/ggge.20071 (2013)

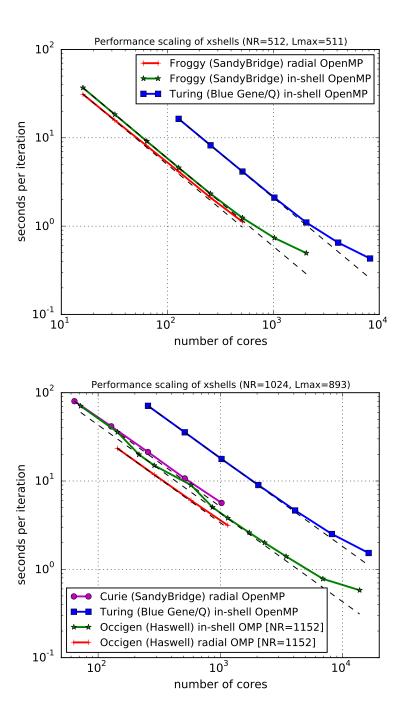


Figure 1.1: Performance scaling of XSHELLS, on french supercomputers with different architectures: SandyBridge on Froggy (CIMENT) and Curie (thin nodes, TGCC); Haswell on Occigen (CINES); and $Blue\ Gene/Q$ on Turing (IDRIS). The ideal scaling for each case is represented by the dashed black lines. Top: geodynamo simulation with $N_r = 512$ radial grid points and spherical harmonics truncated after degree $L_{max} = 511$. Bottom: geodynamo simulation with $N_r = 1024$ or 1152 and $L_{max} = 893$.

Chapter 2

Setting up the simulation

Example configuration files can be found in the problems directory.

2.1 Run-time options: xshells.par

The file xshells.par is a simple text file. Each line may contain a single statement like var = expression, or a comment starting with #. A simple math parser allows to use convenient expressions like sqrt(4*pi/3).

All the following features can be set in xshells.par. There is no need to recompile if this file is changed, as it is read and interpreted at program startup.

2.1.1 Equations and controlling parameters

XSHELLS can time-step the Navier-Stokes equation in a rotating reference frame. Optionally it can include (i) a buoyancy force in the Boussinesq approximation, where the buoyancy obeys an advection-diffusion equation; and (ii) a Lorentz (or Laplace) force for conducting fluids where the magnetic field obeys the induction equation. Precisely, the following equations can be time-stepped by XSHELLS:

$$\partial_t \mathbf{u} + (2\Omega_0 + \nabla \times \mathbf{u}) \times \mathbf{u} = -\nabla p^* + \nu \Delta \mathbf{u} + (\nabla \times \mathbf{b}) \times \mathbf{b} + c \nabla \Phi_0$$
 (2.1)

$$\partial_t \mathbf{b} = \nabla \times (\mathbf{u} \times \mathbf{b} - \eta \nabla \times \mathbf{b}) \tag{2.2}$$

$$\partial_t c + \mathbf{u} \cdot \nabla(c + C_0) = \kappa \Delta c \tag{2.3}$$

$$\nabla \mathbf{u} = 0 \tag{2.4}$$

$$\nabla \mathbf{b} = 0 \tag{2.5}$$

where

- **u** is the velocity field.
- c is a codensity (or temperature, or buoyancy) in the Boussinesq formulation.

- $\sqrt{\mu_0 \rho}$ **b** is the magnetic field (ρ and μ_0 are the fluid density and magnetic permeability, but are not relevant for this equation set).
- ν is the kinematic viscosity of the fluid and is set by the variable nu in xshells.par.
- $\eta = (\mu_0 \sigma)^{-1}$ is the magnetic diffusivity of the fluid (σ is its conductivity) and is set by the variable eta in xshells.par. Diffusivity $\eta(r)$ depending on shell radius are also supported (see sec. 2.2.4).
- κ is the thermal diffusivity of the fluid and is set by the variable kappa in xshells.par.
- Ω_0 is the rotation vector of the reference frame, which is usually along the vertical axis $\mathbf{e_z}$. It is set by the variable OmegaO in xshells.par, while the angle (in radians) between $\mathbf{e_z}$ and Ω_0 is set by OmegaO_angle (0 by default). Note that Ω_0 is always in the x-z plane ($\phi=0$).
- Φ_0 is the gravity potential (independent of time), controlled by field phi0 in xshells.par.
- C_0 is the imposed base concentration (or temperature) profile, controlled by field tp0 in xshells.par.
- p^* is the dynamic pressure deviation (from hydrostatic equilibrium), which is eliminated by taking the curl of equation 2.1.

Equation 2.1 (respectively 2.2 and 2.3) is time-stepped when u (respectively b and tp) is set to an initial condition in xshells.par. Disabling an equation is as easy as removing or commenting out the corresponding initial condition in xshells.par.

Example If the following lines are found in xshells.par:

```
nu = 1.0
eta = sqrt(10)
Omega0 = 2*pi*1e3

u = 0
b = 0
#tp = 0
```

then the viscosity is set to $\nu = 1.0$, the magnetic diffusivity is set to $\eta = \sqrt{10}$, and the rotation rate is set to $\Omega_0 = 2\pi \times 10^3$. The Navier-Stokes (2.1) and the induction equation (2.2) will be time-stepped, but not the concentration (or temperature) equation (2.3), simulating an isothermal fluid.

Note that it is up to the user to choose dimensional or non-dimensional control parameters. A notable exception is the magnetic field, which is always scaled to the same unit as the velocity field.

Internal representation of vector fields

Vector fields are represented internally using a poloidal/toroidal decomposition:

$$\mathbf{u} = \nabla \times (T\mathbf{r}) + \nabla \times \nabla \times (P\mathbf{r}) \tag{2.6}$$

where \mathbf{r} is the radial position vector, and T and P are the toroidal and poloidal scalars respectively. This decomposition ensures that the vector field \mathbf{u} is divergence-free.

The scalar fields T and P for each radial shell are then decomposed on the basis of spherical harmonics.

2.1.2 Boundary conditions

Magnetic field boundary conditions are that of an electrical insulator outside the computation domain, with or without external sources of magnetic field (see section 2.1.3 for externally imposed magnetic fields).

Temperature or buoyancy boundary conditions are either fixed temperature (defined by the C_0 profile) or fixed flux (defined by $\partial_r C_0$).

Velocity boundary conditions can be zero, no-slip (with arbitrary prescribed velocity at the boundary) or stress-free.

The inner and outer boundary conditions can be chosen independently. The BC_U (for velocity) and BC_T (for temperature/concentration) entries in xshells.par allow to select the appropriate boundary conditions.

Example

The following lines in xshells.par define zero velocity and fixed temperature boundary condition at the inner boundary, and no-slip and fixed flux boundary condition at the outer boundary.

2.1.3 Initial conditions and imposed fields

Predefined fields

Several predefined fields are defined in xshells_init.cpp. The command ./list_fields prints a list of these predefined fields, with their name in the first column. You can simply

use this name in the xshells.par file to define an initial condition. You can also add your own by editing xshells_init.cpp.

Imposed fields are only supported for the gravity potential phi0 and for the basic state of temperature/concentration tp0. Imposed magnetic fields can be obtained through the appropriate boundary conditions (magnetic fields generated by currents outside the computation domain only). Some predefined magnetic field include these boundary conditions, making them actually *imposed* fields (and are labeled as such).

Example The following lines in xshells.par set up the geodyanmo benchmark initial conditions.

Field files as initial conditions

In addition, any field file can be given as initial condition. If the radial grid is not the same, the field must be interpolated on the new grid. To avoid mistakes, interpolation is disabled by default and must be enabled by interp = 1 (often found near the end of the xshells.par file).

Example The following lines start from the velocity field saved in file fieldU.previous_job, which was performed at different parameters and with a different number of radial grid points.

2.1.4 Forcing

Besides thermal convection, mechanical forcing can be imposed at the boundaries.

Predefined variable a_forcing and w_forcing define the amplitude and frequency of a forcing. The precise nature of the forcing (e.g. differential rotation) must be defined in the xshells.hpp file before compilation (see section 2.2.6).

2.1.5 Spatial discretization

Radial grid

XSHELLS uses second order finite differences in radius. The total number of radial grid points is defined in xshells.par by the variable NR. The radial extent of each field is set using the corresponding R_X variable, which stores a pair of increasing positive real numbers defining the radial extent of the field. The NR grid points will be distributed between radii corresponding to the minimum and maximum of these values. Currently, only the magnetic field can extend beyond the velocity field, modeling conducting solid layers.

Example The following lines in xshells.par define the radial extent of the fields:

```
R_U = 7/13 : 20/13

R_B = 0.0 : 20/13

R_T = 7/13 : 20/13
```

The default grid refines the number of points in the boundary layers, and this refinement can be controlled by the variable N_BL that stores a pair of integers, the first and second being the number of points reserved for the inner and outer boundary layer respectively, reinforcing the normal refinement. The code generating the grid can be found in the grid.cpp file.

Example The following lines in xshells.par define a grid with a total of 100 radial grid points, with 10 and 5 points reserved to the refinement of the inner and outer boundary layer respectively.

```
NR = 100
N_BL = 10,5
```

Alternatively, a radial grid can be loaded:

• from a text file containing the radius of each grid point (increasing) in a separate line.

• from a previously saved field (see section 1.6).

In both cases, simply indicate the filename in the r variable. It will override the NR and N_BL variables.

Example The following line in xshells.par will use the same grid as the field stored in file fieldU_0001.previous

```
r = fieldU_0001.previous # load grid from file
```

Angular grid and spherical harmonic truncation

XSHELLS uses spherical harmonics to represent fields on the sphere:

$$f(\theta, \phi) = \sum_{m=0}^{M} \sum_{\ell=mK}^{L} f_{\ell}^{mK} Y_{\ell}^{mK}(\theta, \phi)$$
 (2.7)

where Y_{ℓ}^{m} is the spherical harmonic of degree ℓ and order m. The expansion uses a K-fold symmetry in longitude (ϕ) and is truncated at maximum degree L and order MK. If K=1 and M=L, it is the standard triangular truncation.

L, M and K are set in xshells.par using the Lmax, Mmax and Mres variables respectively. You must ensure that $L \ge MK$.

The angular grid (spanning the co-latitude θ and longitude ϕ) consists of Nphi regularly spaced points in longitude, and Nlat gauss nodes in latitude. If these are not specified, XSHELLS will choose the values for Nlat and Nphi in order to ensure best performance and no aliasing of modes (Nlat > 3L/2 and Nphi > 3M).

Example These lines limit the spherical harmonic degree to 170. A 3-fold symmetry is used, and the maximum harmonic order is $56 \times 3 = 168$.

```
Lmax = 170  # max degree of spherical harmonics
Mmax = 56  # max fourier mode (phi)
Mres = 3  # phi-periodicity.
```

Most likely, 180 regularly spaced points in longitude and 256 gauss nodes in latitude will be used here.

2.1.6 Time-stepping

XSHELLS uses semi-implicit Crank-Nicolson scheme for the diffusive terms, while the non-linear terms can be handled either by an Adams-Bashforth or a Predictor-Corrector scheme (both second order in time).

The time-step of the numerical integration is set by dt in xshells.par.

The sub_iter variable is half the number of time-steps taken before any diagnostic is computed and written to file energy.job or displayed on screen. For example, if sub_iter = 50, then 100 time-steps will be performed before computing and printing some diagnostics. This is then called an iteration.

The iter_max variable is the total number of iterations, so that the total number of time-steps before the code will stop is iter_max $\times 2 \times$ sub_iter.

By setting $\mathtt{dt_adjust} = 1$, an (experimental) automatic time-step adjustment can be turned on. In that case, the number of sub-iterations $\mathtt{sub_iter}$ is also adjusted so that an iteration is a constant time span, and thus the outputs happen at fixed time intervals $\Delta T = 2 \times \mathtt{sub_iter} \times \mathtt{dt}$.

Finally, iter_save controls the number of iterations before a (partial) snapshot is saved to disk.

Example The following lines in xshells.par will use a time-step of 0.01 for the numerical integration:

Output will occur every $\Delta T = 0.01 \times 25 \times 2 = 0.5$ time units (an iteration). The program will stop after iter_max=300 outputs (or iterations), spanning a total physical time of $t_{end} - t_{start} = 150.0$. Partial fields are saved every 10 iterations, or every 5.0 physical time units, if movie = 1 is set (see below).

2.1.7 Real time plotting

At each iteration, XSHELLS can plot the kinetic and magnetic energies as a function of time, using gnuplot. Note that the plots are refreshed every iteration, but no more than once every two seconds. This allows to follow program execution in real-time, but might not be useful for high performance distributed jobs. The interaction with gnuplot can be turned off entirely by passing the --disable-gnuplot option to ./configure.

The variable plot in the file xshells.par allows some flexibility:

- plot = 0: disables plotting.
- plot = 1: shows plot on display; if no display found, write to png file instead. This is the default.

- plot = 2: saves plot to png file only.
- plot = 3: shows plot on display (if available) and also saves plot to png file.

2.1.8 Time lapse field snapshots

The parameter movie controls the field snapshots, saved every iter_save iterations (see above).

- movie = 1: the initial field is saved to fieldX_0000.job, after iter_save iterations the fields are saved to fieldX_0001.job, then fieldX_0002.job, and so on.
- movie = 0: no such fields are saved.
- movie = 2: in addition to the snapshots of the fields, the time-average since the last snapshot is also computed and saved.

The parameter prec_out controls the precision (single or double precision) of the snap-shot files. In order to save disk space, the snapshots are saved in single precision by default (prec_out = 1), which should be enough to make plots, but not suitable for restarting or computing gradients. If you need double precision snapshots, set prec_out = 2. To save further disk space, snapshots can be truncated at lower spherical harmonic degree and order, using the parameters lmax_out and mmax_out, respectively.

The snapshots can then be post-processed with xspp to produce plots or movies (see 3).

Example The following lines in xshells.par instruct the program to output snapshots and time-averages of the axisymmetric component of the fields, every iter_save iterations:

2.1.9 Checkpointing and restarting capabilities

By default after initialization the job starts at the beginning (iteration 0). It is easy to start a new job by using as input fields the field files written by a previous job, effectively continuing that job.

Sometimes, it is useful to automatically continue a stopped or killed job (e.g. in batch execution environments found in high-performance computing machines). By default, a full resolution snapshot is written to disk every four hours. Parameters found in xshells.par allow to tune that interval, and enable restart from these checkpoint automatically when the program is run again.

For increased safety, when writing a new checkpoint (or backup) to file fieldX.jobname, the previous one is first renamed to fieldX_back.jobname. This file may allow to continue a simulation in case of an unexpected termination of the program while writing the new checkpoint.

If restart = 1, the program will start by looking in the current directory for checkpoint files that have been saved by a previous run with the same job name, and use these to resume that job.

Example

Suppose that on a supercomputer, the wall time of the jobs is limited to 24 hours. In order to run a job that spans several days, the following lines in xshells.par allow a job to be resumed by simply resubmitting it:

```
restart = 1  # 1: try to restart from a previous run with  # same name. 0: no auto-restart (default).

backup_time = 470  # ensures that full fields are saved to disk at  # least every backup_time minutes, for restart.

nbackup = 3  # number of backups before terminating program  # (useful for time-limited jobs).

# 0 = no limit (default)
```

In addition, a checkpoint (or backup) is written to disk every 470 minutes, and the program will stop after writing the third backup, thus leaving 30 minutes of safety time for program initialization and file writing time. In case of a system failure, no more than 470 minutes of computing time will be lost.

2.1.10 Advanced options

The time integration scheme can be chosen at runtime. The default is a 2nd order Adams-Bashforth scheme (AB2). In addition, a corrector step can be enabled after the explicit AB2, leading to a second order predictor-corrector scheme. Note that the latter option is more accurate but is two times slower.

Put time_scheme = 1 in the xshells.par file to increase accuracy with a predictor-corrector scheme.

```
time_scheme = 0  # 0: AB2 (default); 1: AB2+PECE (2x slower);
```

Fine tuning of the automatic time-step selection is possible through some variables.

C_u is a safety factor for the standard CFL (based on the velocity and the grid size). In some cases C_u = 1 gives good results, but in other cases a more stringent value is needed (e.g. C_u = 0.1). C_vort and C_alfv control the time-step adjustment (active if dt_adjust=1), regarding vorticity and Alfvén criteria, respectively. The lower the values of C_vort and C_alfv, the smaller the adjusted time step will be.

In addition, to prevent too many time step adjustments, if dt_tol_lo < dt/dt_target < dt_tol_hi, no time-step adjustment is done.

```
Example

C_u = 0.1  # default: 0.1

C_vort = 0.1  # default: 0.1

C_cori = 0.1  # default: 0.1

C_alfv = 1.0  # default: 1.0

dt_tol_lo = 0.8  # default: 0.8

dt_tol_hi = 1.1  # default: 1.1
```

Variable spherical harmonic degree truncation is controlled by setting the variable rsat_ltr in xshells.par. This is possible only if XSHELLS was compiled with variable truncation enabled (see section 2.2.5).

Spectral convergence of fields is checked by comparing the maximum of the end of the spectrum (four last modes) with the maximum of the spectrum. The first few modes are ignored (because their amplitude can be related directly to forcing or imposed fields). The variables $sconv_min$ and $sconv_min$ that can be set in shells.par define the first spherical harmonic degree and order respectively that are considered when checking spectral convergence in the ℓ or m spectra. The default value is 3 for both variables. Setting a value larger than lmax disables spectral convergence checks. Note also that the convergence checks are skipped when only a few modes are computed.

```
Example
sconv_lmin = 3  # ignore l=0-2 for spectral convergence.
sconv_mmin = 1  # ignore m=0 for spectral convergence.
```

The SHTns library can be controlled in terms of algorithm used for transforms, and in terms of polar optimization threshold.

The sht_type variable allows to constrain the transform method used:

- sht_type = 0 : select fastest method using a classic Gauss-Legendre grid (default setting).
- sht_type = 1 : select fastest method, allowing also regular grids (with DCT) which may be faster for small Mmax.
- sht_type = 2 : impose a regularly spaced grid (not recommended as it is often slower).
- sht_type = 3 : force a regularly spaced grid using DCT (not recommended as it is often slower).
- sht_type = 4 : debug mode; initialization time is reduced, but a default method is used (no selection of fastest method).
- sht_type = 6 : use a Gauss-Legendre grid with on-the-fly computation (preferred when parallel execution or big resolutions).

Finally, the polar optimization threshold can be adjusted with sht_polar_opt_max, the value below which coefficients near the pole are neglected. To give the reader some more insight, here are a some possible values and their impact:

- sht_polar_opt_max = 0 : no polar optimization.
- sht_polar_opt_max = 1e-14 : very safe optimization (default).
- sht_polar_opt_max = 1e-10 : safe optimization.
- sht_polar_opt_max = 1e-6 : aggressive optimization.

2.2 Compile-time settings: xshells.hpp

All the following settings can be found in xshells.hpp. You have to recompile the program if you change this file.

2.2.1 Custom diagnostics

Enable by uncommenting:

#define XS_CUSTOM_DIAGNOSTICS

In addition to the total energy of the three fields U, B and T, which are saved every 2 sub_iter time steps (see section 2.1.6), custom diagnostics can be defined in the $custom_diagnostic()$ function, found in the xshells.hpp file. They are computed every iteration and saved in energy.job after the energies. The best is to look at the existing diagnostics defined in the $custom_diagnostic()$ function to add your own.

2.2.2 Variable time-step

Enable compilation of variable time-step code by uncommenting:

#define XS_ADJUST_DT

In addition, variable time-step must also be allowed by setting dt_adjust = 1 in file xshells.par (see also section 2.1.6).

2.2.3 Linearized Navier-Stokes

To replace the equations with their linearized version (no $(\nabla \times \mathbf{u}) \times \mathbf{u}$, no $(\nabla \times \mathbf{b}) \times \mathbf{b}$, no $\mathbf{u} \cdot \nabla c$), uncomment:

#define XS_LINEAR

Note that spherical harmonic transforms are not needed anymore if there are no base fields, leading to a much faster program. Base fields are also supported, and can be set using u0, b0 and tp0 in the xshells.par file. See also the example located in problems/taw.

2.2.4 Variable conductivity

In equation 2.2, conductivity can depend on radius r. To define a conductivity profile $\eta(r)$, uncomment:

#define XS_ETA_PROFILE

and then define your profile in the calc_eta() function, found in the xshells.hpp file. The purpose of calc_eta() is simply to fill the array etar with values of the magnetic diffusivity for every radial shell. The program handles continuous profiles as well as discontinuities in $\eta(r)$ properly and automatically.

2.2.5 Variable spherical harmonic degree truncation

In order to compute in a full sphere and avoid problems near r = 0, the spherical harmonic expansion must be truncated at low degree near r = 0. XSHELLS can truncate the spherical harmonic expansions at a different degree for each shell, when the following line is uncommented in xshells.hpp:

#define VAR_LTR 0.5

The value of VAR_LTR (0.5 in the line above, which is a good choice for full-sphere computations) is used as α in the formula to determine the truncation degree ℓ_{tr} :

$$\ell_{tr}(r) = L_{max} \sqrt{\frac{r}{\alpha r_{max}}} + 1$$

where L_{max} is defined by Lmax in xshells.par and r_{max} is the radius of the last shell. Note that ℓ_{tr} cannot exceed L_{max} .

Note also that α can be overridden by the rsat_ltr variable in xshells.par.

2.2.6 Boundary forcing

Amplitude and frequency are set at runtime by a_forcing and w_forcing in the xshells.par file.

Time dependent boundary forcing are defined in the function calc_Uforcing(), found in the xshells.hpp file. In this function you must define a name for your forcing through the macro U_FORCING. The angular velocity of the solid bodies (defining the boundary of the fluid shell) can be set in this function. It will be used as a boundary condition for the flow if no-slip boundaries are used (see section 2.1.2).

See the example found in the problems/couette/ folder for more details, and uncomment the part of the function corresponding to your problem. In particular axial differential rotation of the inner or outer boundary can be used to simulate a spherical Couette flow; equatorial differential rotation (or spin-over) can be used to simulate precession or nutation.

Note that the rotation rate of the solid bodies is also used in the induction equation if the magnetic field extends into the solids (conducting solid shells).

Arbitrary stationary boundary flows You can impose arbitrary stationary flows at the solid boundaries. Uncomment:

#define XS_SET_BC

and change the set_U_bc() function found in xshells.hpp according to your needs. Note that the boundary conditions for the poloidal velocity field is stored in the shell beyond the first or last fluid shells (respectively NG-1 and NM+1). See for example the xshells.hpp file in the problems/full_sphere/ folder. Note that the solid should not be conducting if this feature is used, as no corresponding solid flow will be generated.

Chapter 3

Post-processing with xspp

Fields are stored in binary files (see 1.6), using a custom format. They can be handled after the simulation by the xspp command line program. Alternatively, the pyxshells python module can also read, write and handle these files (see section 3.4).

3.1 Using the xspp command-line tool

Compile the program by typing make xspp. Invoking it without arguments (by running ./xspp) will print a help screen including the commands and their syntax.

Example The following will display information about the file fieldU.job (resolution, precision, time of the snapshot, ...):

```
./xspp fieldU.job
```

To compute the energy and maximum value of the curl of the field:

```
./xspp fieldU.job curl nrj max
```

To extract the field values along a line spanning the x-axis from x = -1 to x = 0.8, and also display total energy of field:

```
./xspp fieldU.job line -1,0,0 0.8,0,0 nrj
```

Add two fields and save the result to a new file (the first file will set the resolution for the result):

```
./xspp fieldT_0004.job + fieldT0.job save fieldT_total_0004.job
```

Extract only a given range of spherical harmonic coefficients (2 to 31) and computes the corresponding energy:

```
./xspp fieldB.job llim 2:31 nrj
```

Note that xspp is not parallelized using MPI, so that for very big cases you might run out of memory (although it can operate out-of-core – without actually loading the whole file in memory – in some cases). As a workaround you can always reduce the spherical harmonic truncation while reading your big files with the llim option (see example avobe).

3.2 Extract and plot 2D slices

One of the most common usage for xspp is to extract two-dimensional slices of the 3D data stored in spectral representation in the field files. Four types of 2D slices are available:

- Meridian cuts (a plane containing the z-axis), with the merid command;
- Equatorial cuts (the plane z = 0), with the equat command;
- Surface data (on a sphere of given radius r), with the surf command;
- Disc cuts (an arbitrary plane), with the disc command;

When these commands are given to xspp, it will write text files corresponding to the required cuts. They can then be loaded and displayed using matlab, octave or python with matplotlib (see next sections).

Example A meridian cut at $\phi = 0$:

./xspp fieldU.job merid

An equatorial cut, and a meridian cut at $\phi = 45$ degrees, of the vorticity (curl of U)

./xspp fieldU.job curl equat merid 45

Extract the field at the spherical surface closest to r = 0.9, using only the symmetric components.

./xspp fieldU.job sym 0 surf 0.9

Make a cut at z = 0.7, using 200 azimuthal points, with field truncated at harmonic degree 60:

./xspp fieldU.job llim 0:60 disc 200 0,0,0.7

3.2.1 plotting with matlab/octave

Matlab or Octave scripts are located in the matlab dierectory. There are scripts to load and plot cuts obtained with xspp.

Example Produce a meridian cut with xspp:

```
./xspp fieldU.job merid
```

Then, from octave (or matlab), load and plot the ϕ -component of the field in this meridional slice:

```
> [Vphi,r,theta] = load_merid('o_Vp.0');
```

> plot_merid(r,theta,Vphi)

3.2.2 plotting with python/matplotlib

The python module xsplot is provided to load and display cuts produced by xspp. It can be used interactively or within scripts. Such Python scripts using matplotlib and xsplot are located in the matplotlib dierectory, and can be called from command line. xsplot can also be used directly from command line and will guess the type of cut of your file and display it accordingly.

The python module should be installed by calling make install-py, or explicitly python setup.py install --user from the python subdirectory. In addition, it is con-

venient to copy the small script python/xsplot in your path, so that you can invoke xsplot from any directory.

Example Produce a meridian and an equatorial cut with xspp:

```
./xspp fieldU.job merid equat
```

From command prompt, quickly load and plot all three components in cylindrical coordinates of the field in this meridional slice, as well as in the equatorial plane.

```
xsplot o_Vs.0 o_Vp.0 o_Vz.0 o_equat
```

Alternatively, from an Ipython interpreter (or notebook, or script), load and plot the ϕ -component of the field in the meridional and equatorial slices:

```
> import xsplot
> r,theta,Vphi = xsplot.load_merid('o_Vp.0')
> xsplot.plot_merid(r,theta,Vphi)
> s,phi,Vs,Vp,Vz = xsplot.load_disc('o_equat')
> xsplot.plot_disc(s,phi, Vp)
```

Several useful scripts for basic and advanced plotting can be found in the matplotlib directory.

Plotting time-dependent quantities

Time-dependent quantities, such as the energies and other custom diagnostics which are stored in the energy.job file (see section 2.2.1) are also easy to plot with the xsplot module.

```
Example To plot kinetic and magnetic energy as a function of time: xsplot energy.job
```

The load_diags function in the xsplot module can be used to retrieve conveniently any diagnostic. It returns a dictionary of time series for easy plotting.

Example To plot the magnetic to kinetic energy ratio as a function of time:

```
> from pylab import *
> import xsplot
> d = xsplot.load_diags('energy.job')
> t = d['t']
> plot(t, d['Eb']/d['Eu'])  # plot magnetic to kinetic energy ratio
```

3.3 3D visualization with paraview

From the paraview website: ParaView is an open-source, multi-platform data analysis and visualization application. ParaView users can quickly build visualizations to analyze their data using qualitative and quantitative techniques.

Full spatial fields can be saved to XDMF format, which can be loaded by paraview. Note that the HDF5 library is required for this to work, and must be found by the **configure** script. If so, Simply run:

```
make xspp
./xspp fieldB_0004.job hdf5 B_cartesian.h5
```

The file B_cartesian.h5.xdmf describes the cartesian components of the vector field B on a spherical grid that can be read directly by paraview (if prompted for a loader, select 'XDMF').

3.4 Advanced post-processing using pyxshells

For more complex post-processing, xspp may not be enough. The python module pyxshells allows you to quickly write your own scripts to work directly with the spectral fields stored in the field files output by XSHELLS, cast them to spatial domain, and so on.

To install the python modules, type make install-py. You can then import the pyxshells module from any python script.

Chapter 4

Hacking

4.1 Main source files

The main programs (xsbig, xsbig_mpi and xsbig_hyb) all share the same source code:

- xshells_big.cpp is the main source file, including the main loop, and all the solver logic.
- xshells.hpp is where a lot of customization goes on. See section 2.2.
- grid.cpp contains functions related to the radial grid and to the banded matrix linear solver.
- xshells_spectral.cpp contains the definition of the classes used to describe spectral fields (scalar and vector), and the implementation of most associated methods.
- xshells_io.cpp contains methods and functions to load and store fields to file on disk.
- xshells_physics.cpp generation of evolution matrices and computation of physical quantities.
- xshells_init.cpp initialization functions and predefined fields.

The post-processing program xspp uses the previous source files but also:

- xspp.cpp as main source file (instead of xshells_big.cpp)
- xshells_spatial.cpp contains the definition of the classes used to describe spatial fields (scalar and vector), their relationship with spectral representation and associated methods.
- xshells_render.cpp contains method implementations for rendering fields on grids and slices, as well as output to hdf5 files.

4.2 Doxygen

The source code also contains Doxygen documentation comments. Run make docs to generate the documentation targeted at developers and contributors in the doc/html/folder.

4.3 Mercurial repository

To track the changes to the code, the distributed version control system Mercurial is used. The main mercurial repository, found at https://bitbucket.org/nschaeff/xshells allows you to use the latest (unstable) revision (at your own risk). You can also fork it and propose to merge your changes.

Chapter 5

Frequently Asked Questions

- Why is XSHELLS so fast? Short answer: it uses SHTns for spherical harmonic transforms and tries to preserve data locality. A Longer answer can be found in this presentation: http://dx.doi.org/10.6084/m9.figshare.1304532.
- What are the differences with the PARODY code? The numerical methods are basically the same, but their implementations are different. The PARODY code is written in Fortran. The performance and scalability of XSHELLS are better.
- Why is XSHELLS not written in Fortran? Because we don't like Fortran, and we would not be able to get the same level of performance out of a Fortran code. But maybe you could!